

THE CUMULUS CLOUD AS A TRANSIENT

DIABATIC PLUME

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INTROSPECT 2017 (International Workshop on Representation of Physical Processes in Weather and Climate Models) IITM, Pune



CLIMATE SCIENCE

Physicists, your planet needs you

Climatologists highlight cloud mysteries in an attempt to lure physicists to their field.

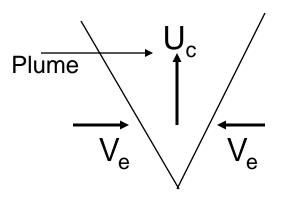
BY QUIRIN SCHIERMEIER

Nature Vol. 520, 9 April 2015



BACKGROUND 1

- Clouds are complex flows involving multiple phases, thermodynamics, microphysics, radiation . . . ? ?
- A central problem in the fluid dynamics of clouds concerns their interaction with the ambient dry air, in particular through entrainment, which is also associated with the dynamic behind shape
- Taylor's entrainment hypothesis for free turbulent shear flows (Taylor 1945, Morton, Taylor, Turner 1956): entrainment velocity V_e ∞ characteristic mean velocity U_c Later refinements: replace U_c by u'_c, (u' w ')^{1/2} etc.
- Often works well for plumes (Turner 1973, 1986 JFM)





- Does not work for cumulus clouds heaps, (the hot cumulus) towers of Riehl (1958), not fans or cones
- ✤ Telford (1975):

Liquid water content remarkably constant across cloud, decreases monotonically from cloud base

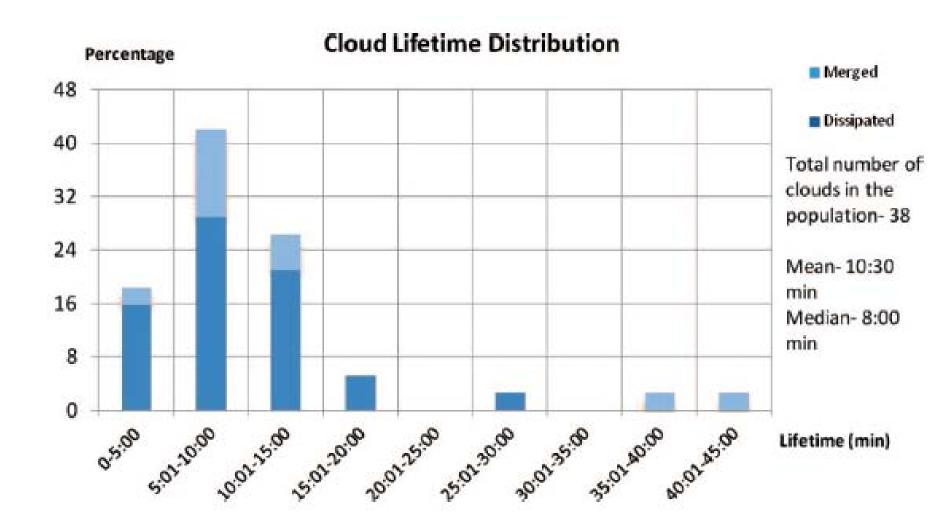
"The problem of explaining infinite horizontal diffusion and zero vertical diffusion"

- Or (from present work on momentum) the other way round?
- Emanuel (1994):

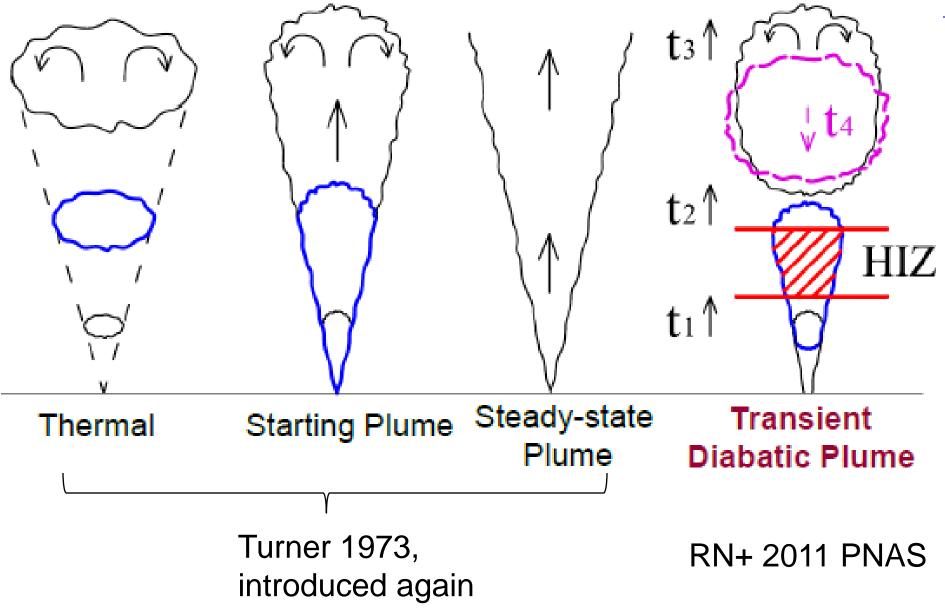
"Early cloud parameterization schemes based on the **similarity** plume model . . . [were] thoroughly discredited by observations".



CLOUD LIFETIMES

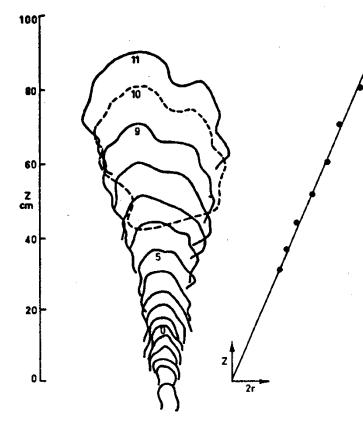








MODELLING CLOUDS



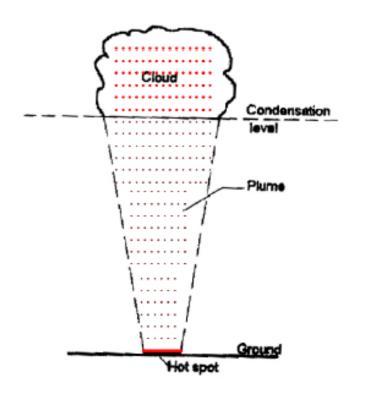
... large convective clouds ... which are not adequately described by similarity theory but for which there is at present no alternative model.

J S Turner 1973 Buoyancy Effects in Fluids

No.

Simulation of cumulus clouds in laboratory

Principle



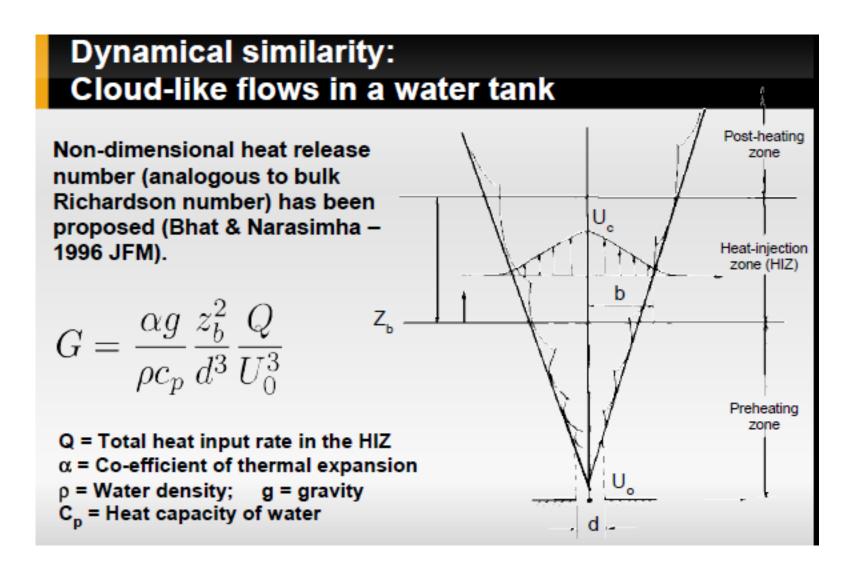
1. Physical model:

Transient turbulent plume/jet of a single-phase 'cloud fluid', with offsource addition of heat to simulate latent heat release due to condensation in natural cumulus clouds

- 2. We work with water, not moist air.
- 3. Shape primarily determined by *large-scale* entrainment processes.

Recent work shows (Narasimha *et al.*, PNAS, 2011) "Clouds are *transient diabatic* plumes"







Dynamical similarity: Cloud-like flows in a water tank

Flow	Width b (m)	Centre-line velocity U (m/s)	$\mathbf{G'} = \frac{\alpha g}{\rho c_p} \frac{Q}{b_b U_b^3}$
Cumulus	500	3 - 4	0.11 - 0.53
Cumulonimbus	1200 - 2500	10 - 25	0.14 - 0.46
Jet/Plume d = 4 mm, z/d = 50, Q = 600 W	21 x 10 ⁻³	38 x 10 ⁻³	0.25

Venkatakrishnan et al. - 1998 Current Science

Re in the experiments is much lower, but jets and plumes are relatively insensitive to Re, for $Re > 10^3 - 10^4$

Dynamical similarity: Cloud-like flows in a water tank

Heat release into the cloud fluid:

~ 1 W/m³ in the atmosphere

What matters: The ratio G

~ (Heat release) / (Energy flux)

- To get same value of G in a water tank as in clouds, we need heat release of O(1 kW) in 5 cm x 5 cm x 10 cm = 250 cm³ = 250 x 10⁻⁶ m³.
- This idea forms the basis for design of the off-source heating mechanism.

(Narasimha 2008)



Non-Dimensional heat release parameter: Bulk Richardson No.

 $G = \frac{\beta g}{\rho C_p} \frac{Q}{bU^3} \sim \frac{heating \ rate}{kinetic \ energy} \quad \text{for jets}$ $\sim \frac{heating \ rate}{buoyancy \ flux} \quad \text{for plumes}$

 β : thermal coefficient of expansion of the cloud fluid (1/K)

g: acceleration due to gravity (m/s²)

ρ and C_p: density (kg/m³) and specific heat (J/kg k) at constant pressure of the ambient fluid

Q: total off-source heating rate (W)

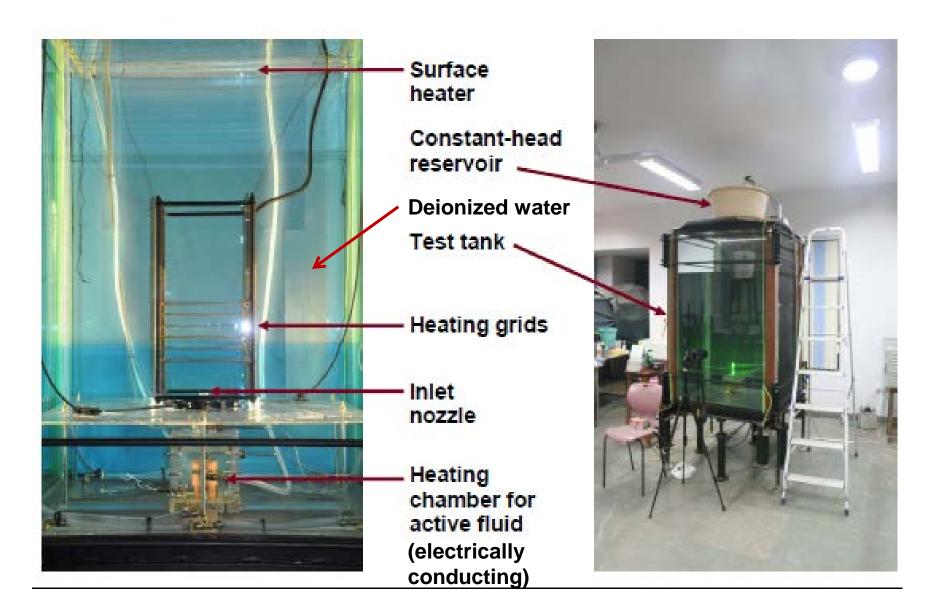
b and U: length and velocity scales (m and m/s)

G can, in principle, vary in space and time

Bhat+narasimha,1996,JFM



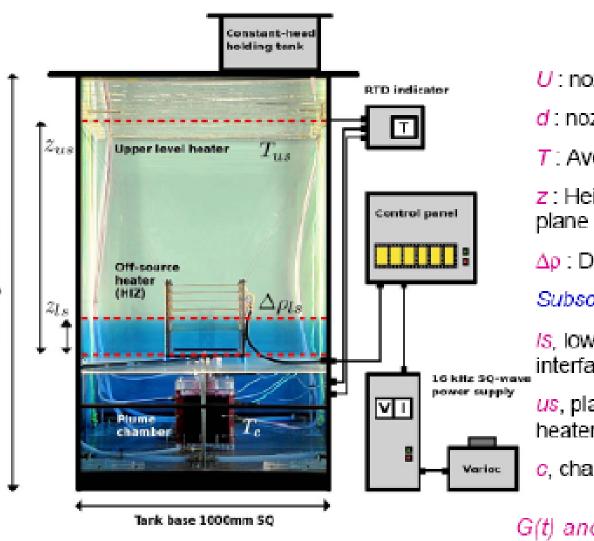
EXPERIMENTAL SET-UP AT JNCASR





EXPERIMENTAL SETUP

Experimental Setup



RTD: Resistance Temperature Detector

$Re = \frac{Ud}{d}$

- U: nozzle-exit velocity
- d : nozzle diameter
- T: Averaged temperature
- z: Height measured from plane of nozzle exit
- $\Delta \rho$: Density difference;

Subscripts:

Is, lower density stratification interface (dash-dot lines);

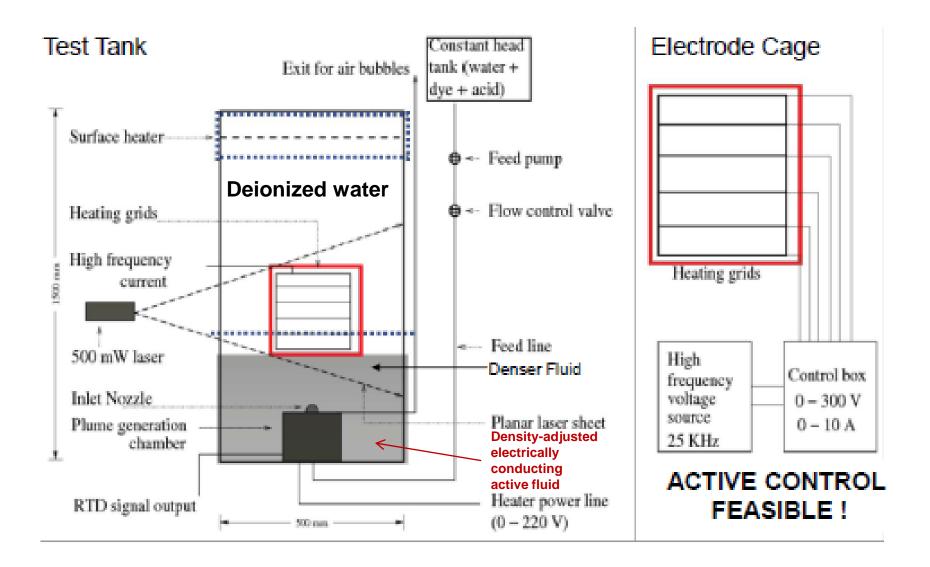
us, plane of free-surface heater;

c, chamber exit.

G(t) and G(z) possible to obtain

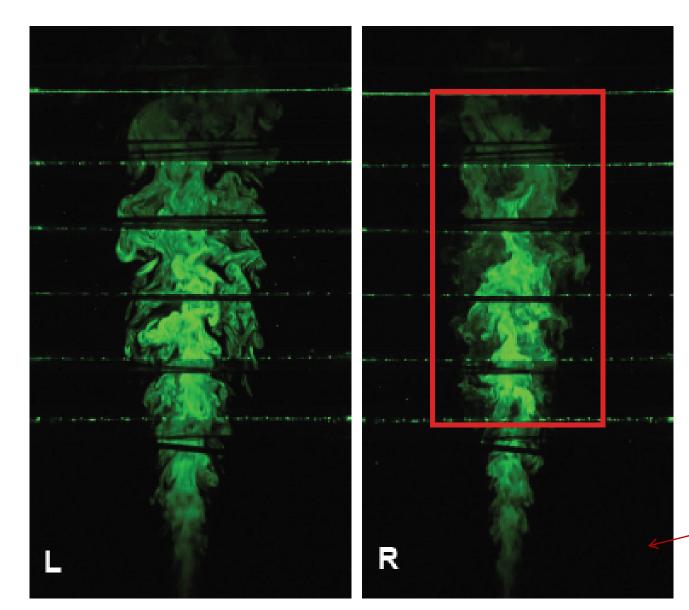


SCHEMATIC OF THE SIMULATOR





AXIAL SECTIONS OF PLUME WITH AND WITHOUT DIABATIC HEATING



• Re = 2250

 Exit velocity at nozzle = 0.28 m/s

 ΔT = 30° C (heating chamber)

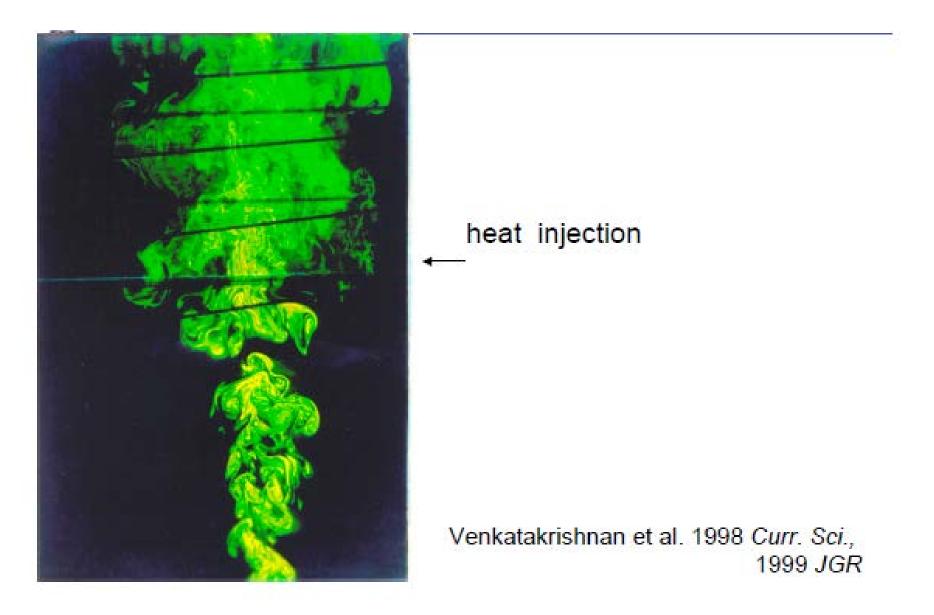
L) Q = 0, G = 0

R) Q = 1350 W G = 13.8

Heat injection zone



HEATING ALTERS FLOW STRUCTURE





Classification as in the International Cloud Atlas (WMO)

Based mainly on appearance

Three genera and three species simulated

Genera: Cumulus Alto- / Strato- cumulus

Species:

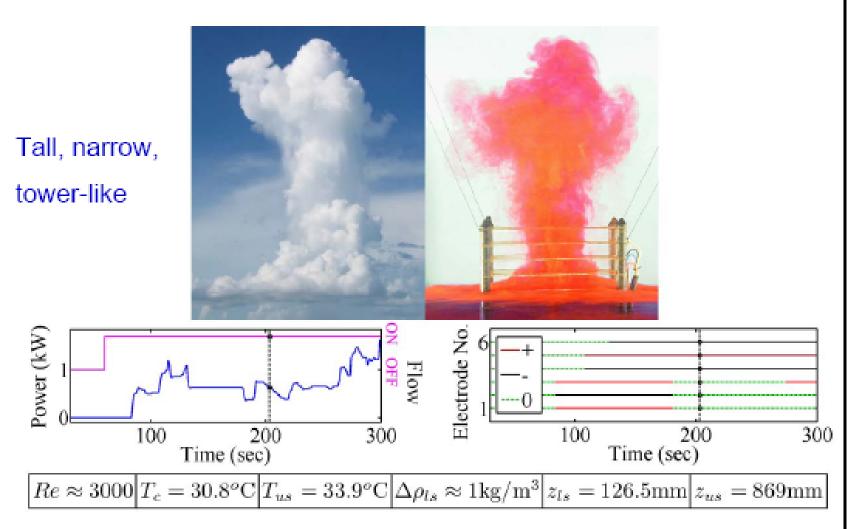
Cu. Congestus Cu. Mediocris Cu. Fractus



COMPARISON WITH REAL CLOUDS Towers and Flowers

Comparison

Cumulus Congestus



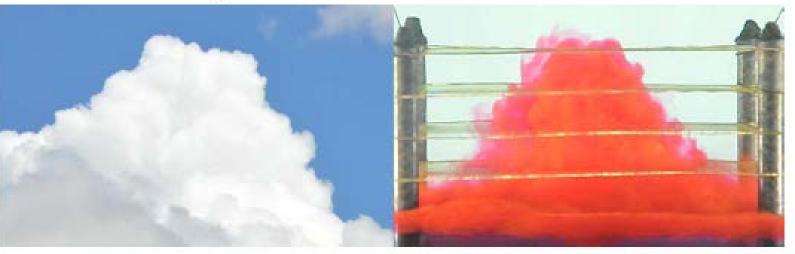
Real Cloud Photo Credit: http://img.photobucket.com/albums/v493/scubastza/Blog%20Stuff/cloud.jpg

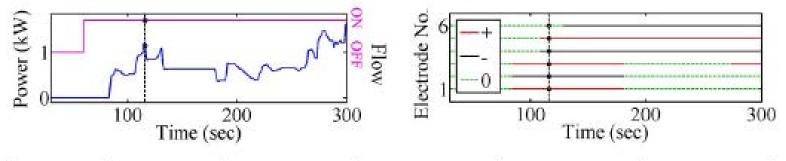


Comparison

Cumulus Congestus

Striking Resemblance





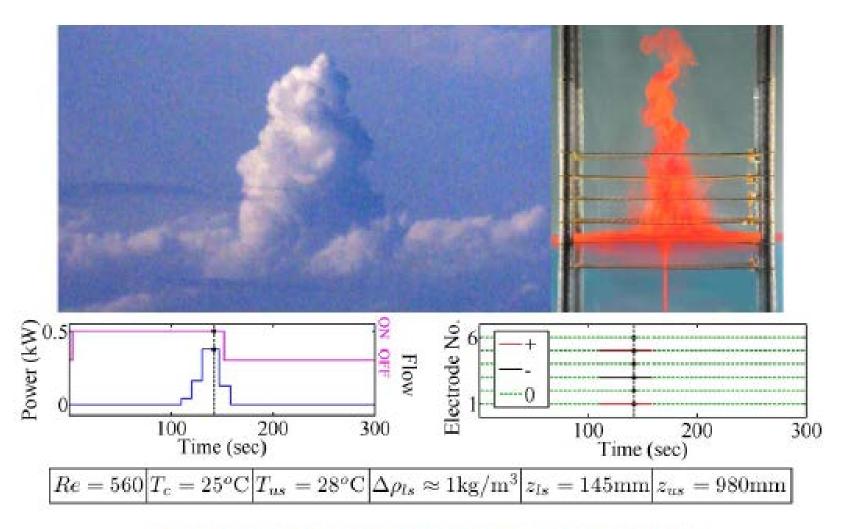
 $\boxed{Re \approx 3000 | T_c = 30.8^{\circ} \text{C} | T_{us} = 33.9^{\circ} \text{C} | \Delta \rho_{ls} \approx 1 \text{kg/m}^3 | z_{ls} = 126.5 \text{mm} | z_{us} = 869 \text{mm}}$

Fluffy, sharp edges, flower-like



Comparison

Cumulus Congestus



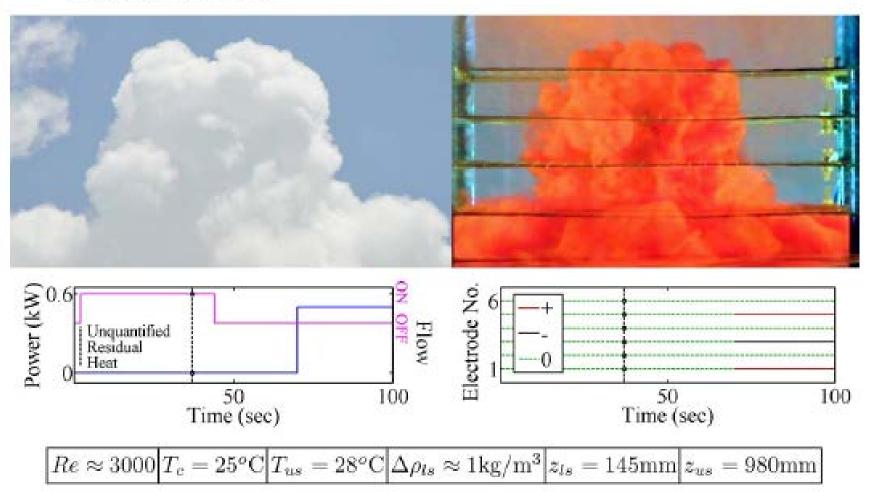
Real Cloud Photo Credit: Aditya Konduri (near Italy; 9-10 km height)



Comparison

Cumulus Congestus

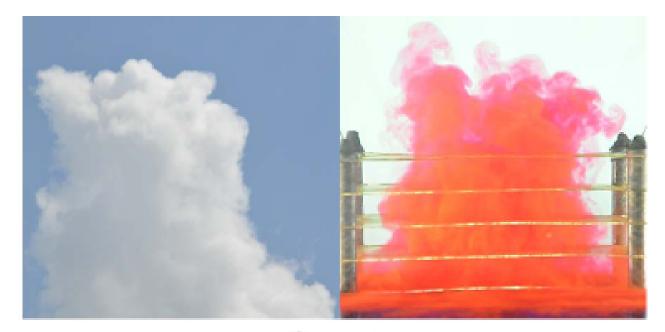
Different Shapes

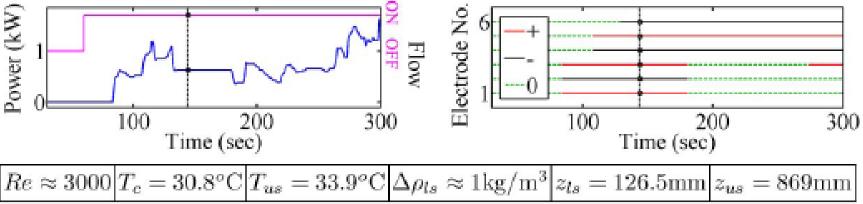




Comparison

Cumulus Congestus

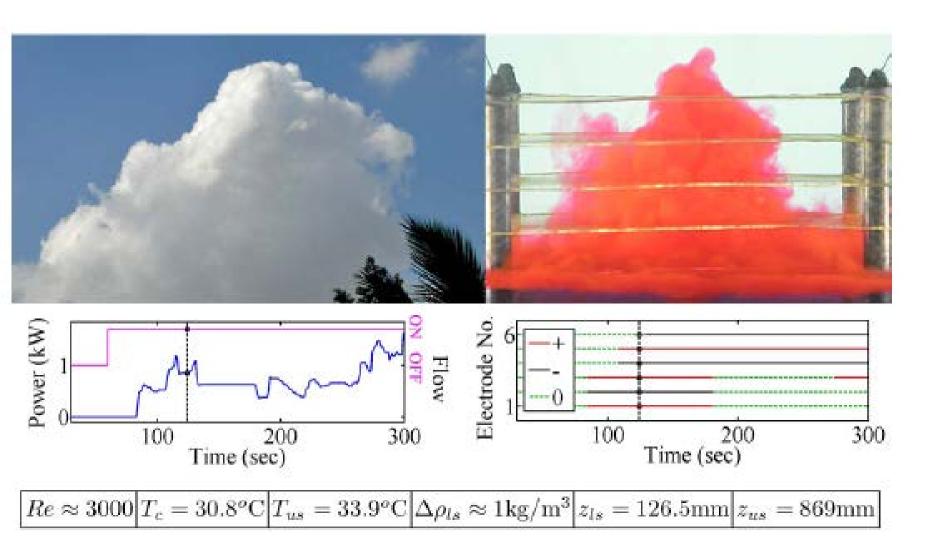






Comparison

Cumulus Congestus



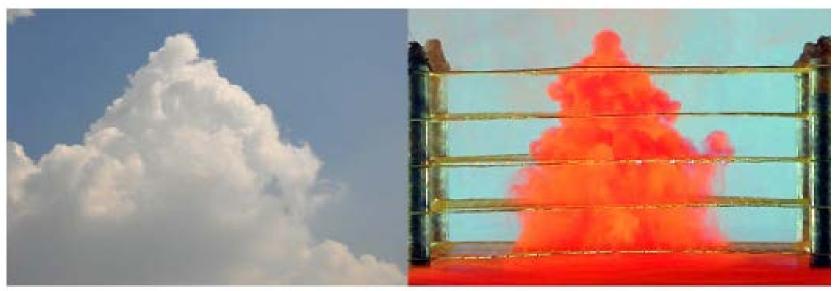


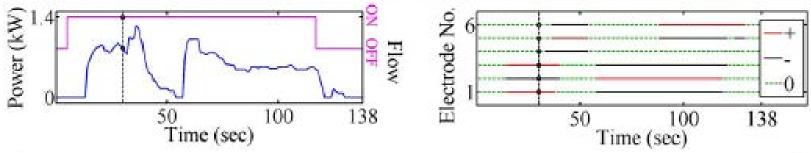
Comparison

Cumulus Congestus

Effect of heating history and distribution

Three instants



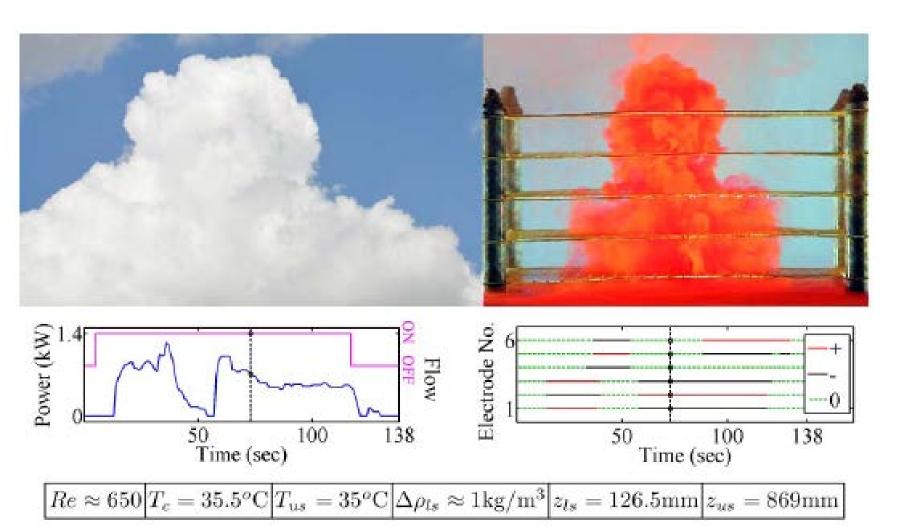


 $Re \approx 650 |T_c = 35.5^{\circ} C |T_{us} = 35^{\circ} C |\Delta \rho_{ls} \approx 1 \text{kg/m}^3 |z_{ls} = 126.5 \text{mm} |z_{us} = 869 \text{mm}$



Comparison

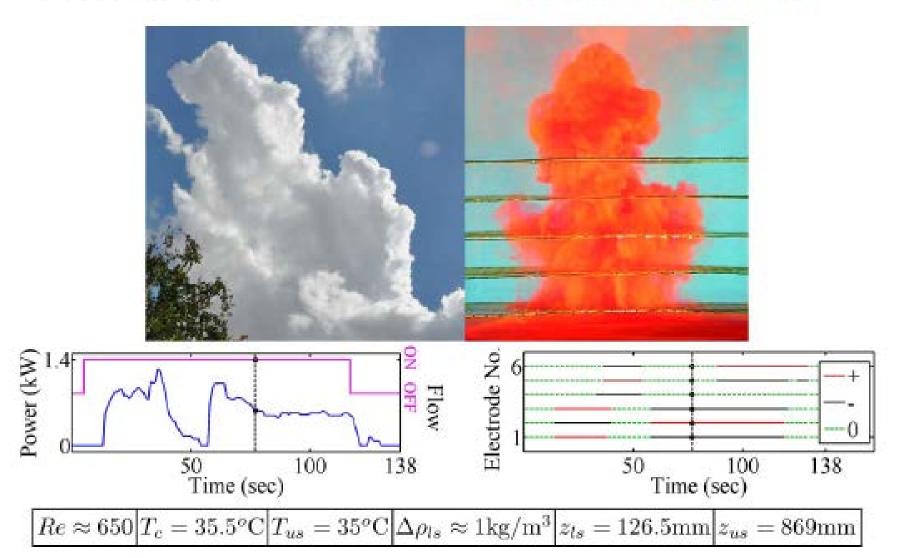
Cumulus Congestus





Comparison

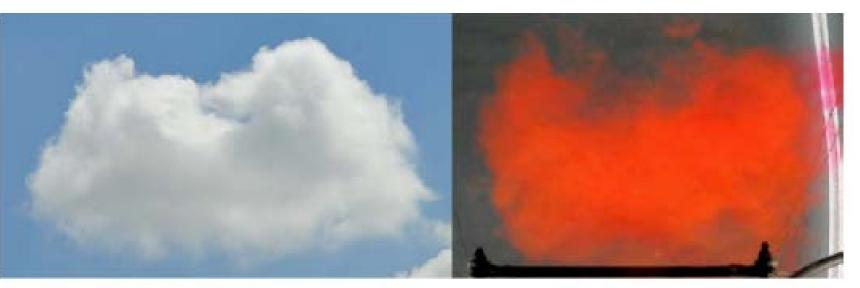
Cumulus Congestus

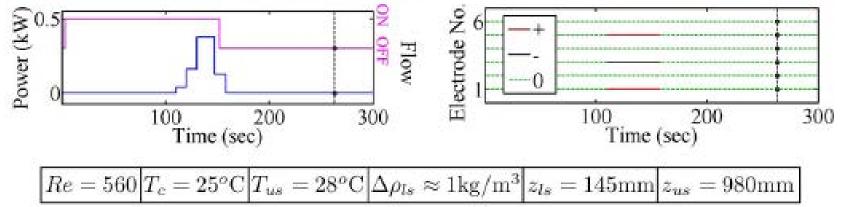




Comparison

Cumulus Mediocris



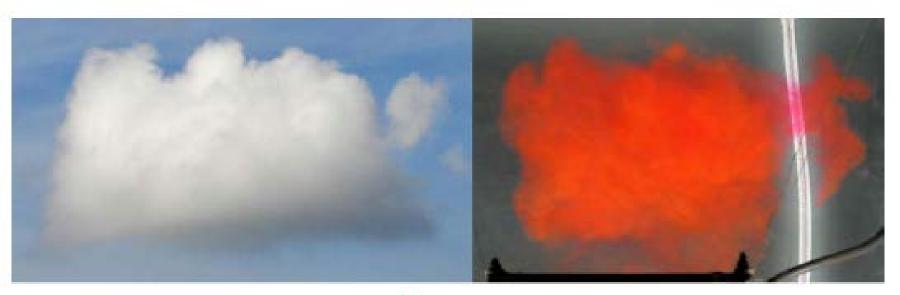


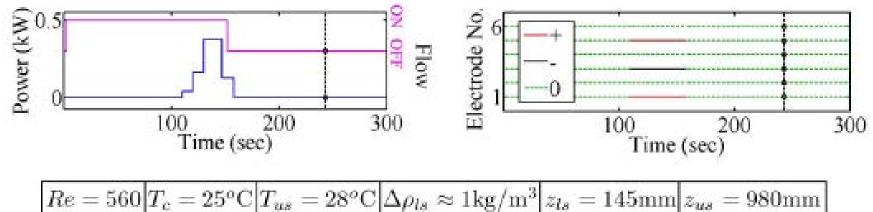
Hovering (slowly sinking), Evaporating



Comparison

Cumulus Mediocris

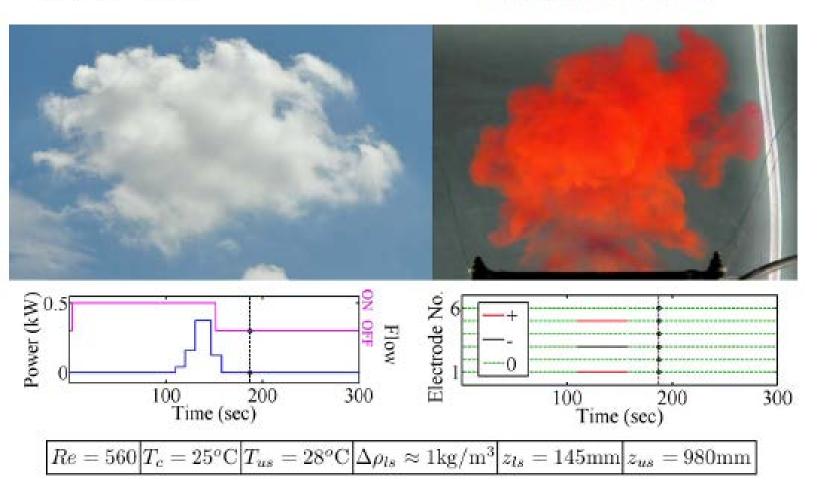






Comparison

Cumulus Fractus

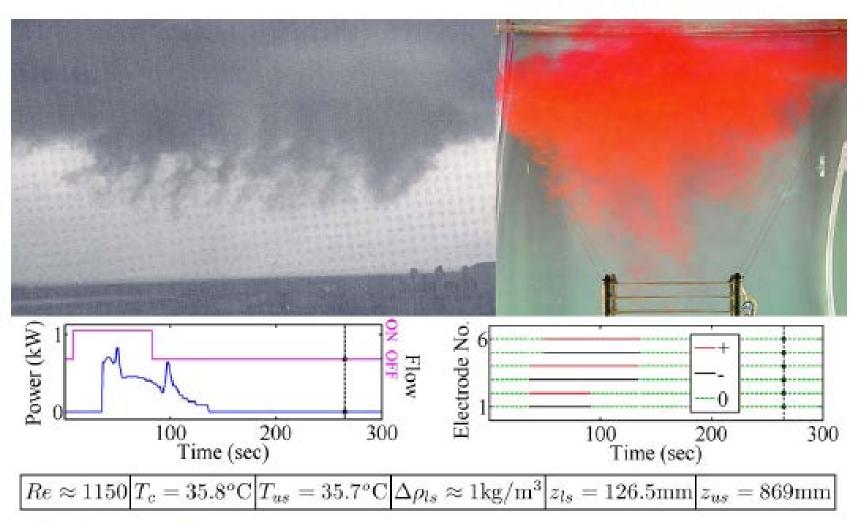


Jagged edges, dissolving stage



Comparison

Cumulus Fractus



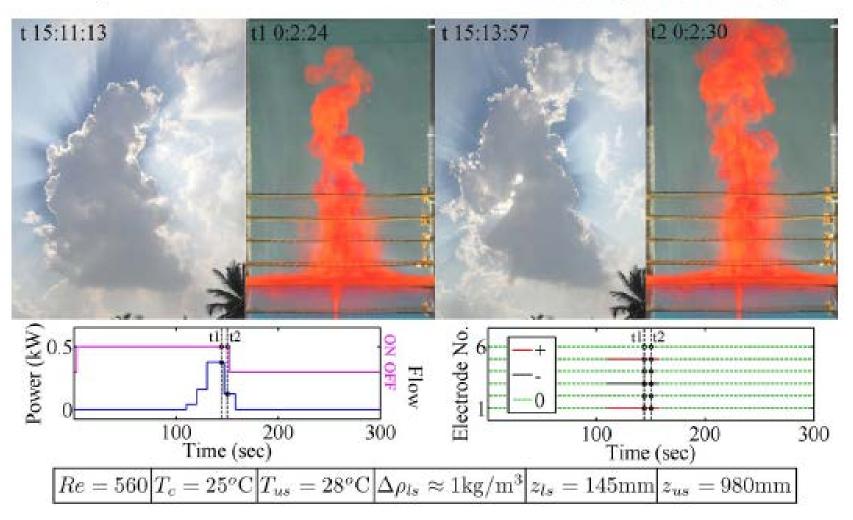
Scud, seen during monsoons

Real Cloud Photo Credit: Scorer Plate 43



Comparison

Cloud-top break away



Simulating cloud processes

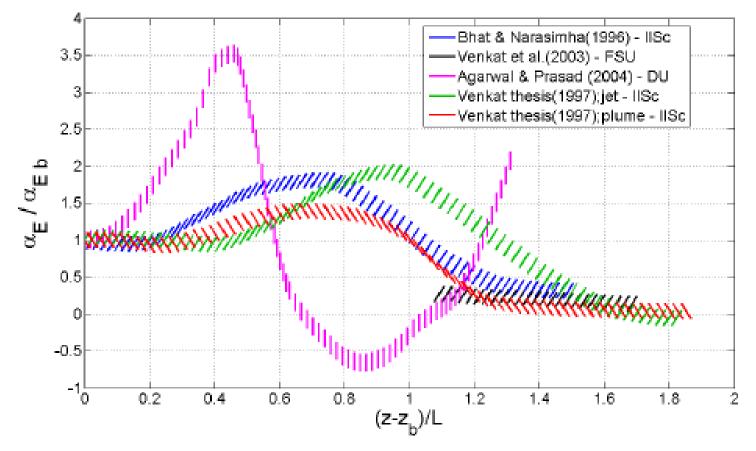


The important parameters identified

- 1. Flow history
- 2. Heating profile history
- 3. Lower and upper stratification (heights and magnitudes)
- 4. Source momentum / buoyancy flux
- Different combinations can give wide variety of cumulus shapes, types, flows



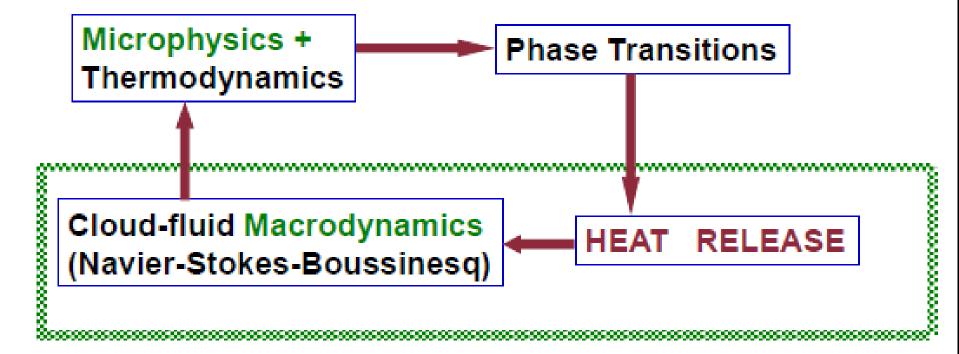
Entrainment Coefficient



 $\alpha_{E} = \frac{dm}{dz} / (2\pi b_{u} U_{c})$

m : integrated mass flux, b_u : velocity width of the flow *U*c : mean centerline velocity *L* : height of HIZ, Z_b : beginning of HIZ



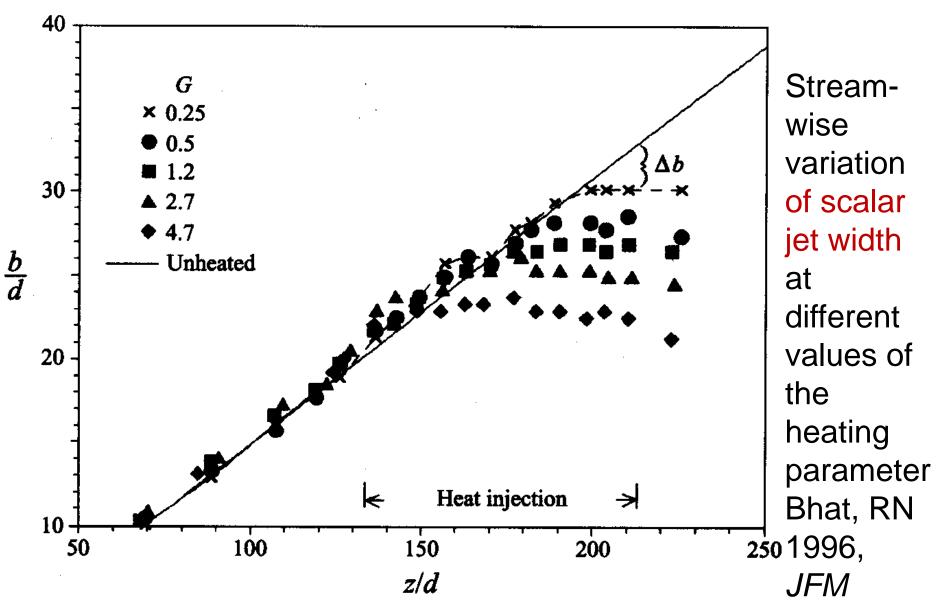




STEADY CLOUD FLOWS

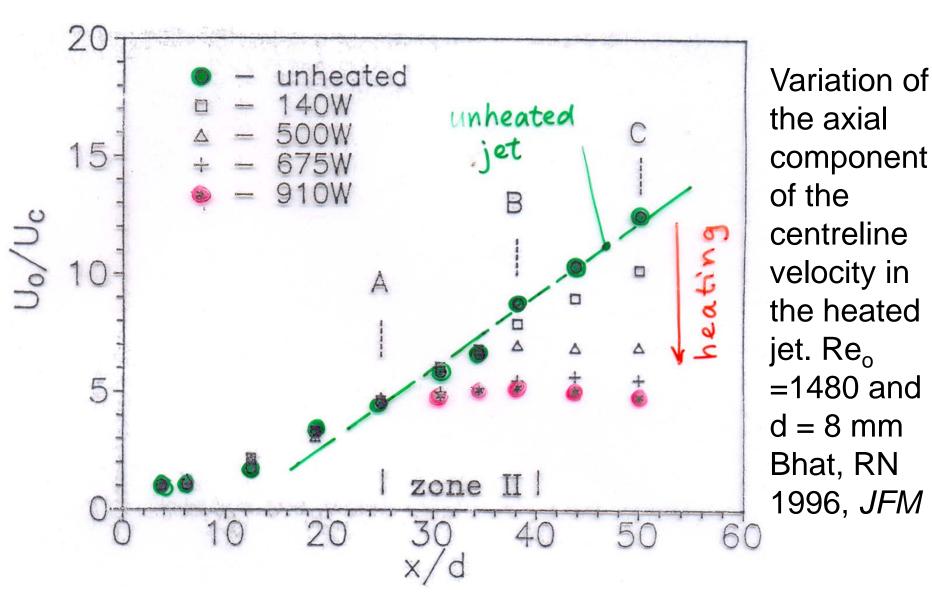


JET WIDTH

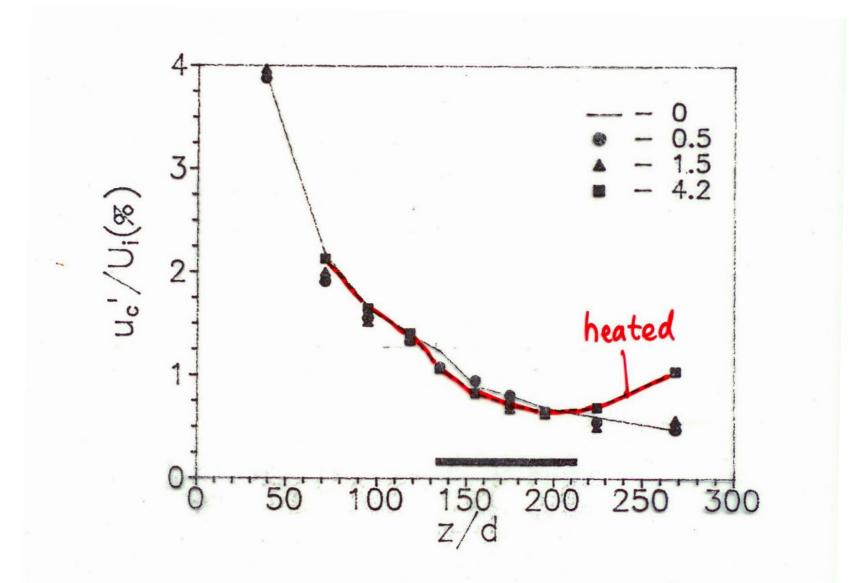




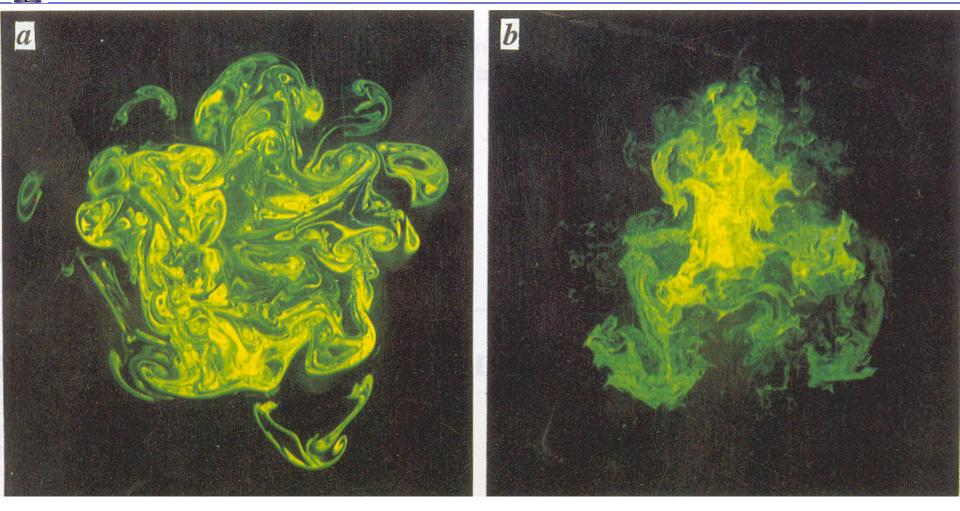
HEATING ACCELERATES FLOW







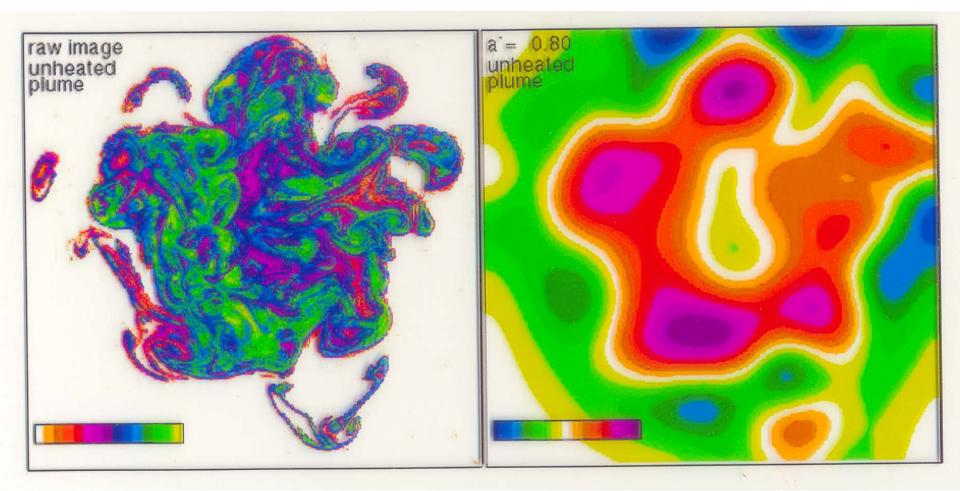
(ORDINARY) PLUME AS IT BECOMES CLOUD-PLUME



Diametral sections of ordinary and cloud plume at z/d = 79.4 Venkatakrishnan et al. 1998 *Curr. Sc.*



WAVELETS REVEAL HIDDEN ORDER, ORDINARY PLUME

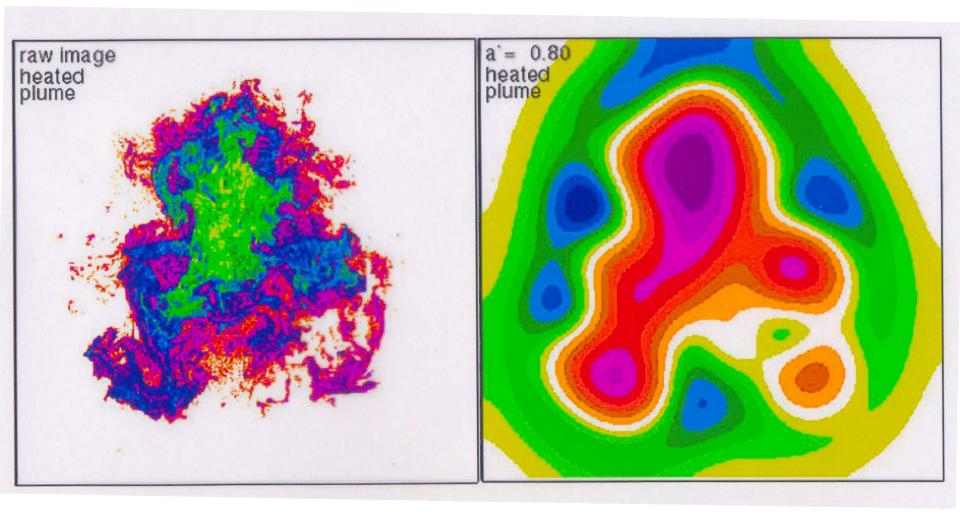


Turbulent chaos conceals lobed vortex ring?

Narasimha et al. 2002 Expts. Fl., Srinivas+ 2007 JoT



CLOUD PLUME: UNMIXED CORE



RN+ 2002 *Expts. Fl.*

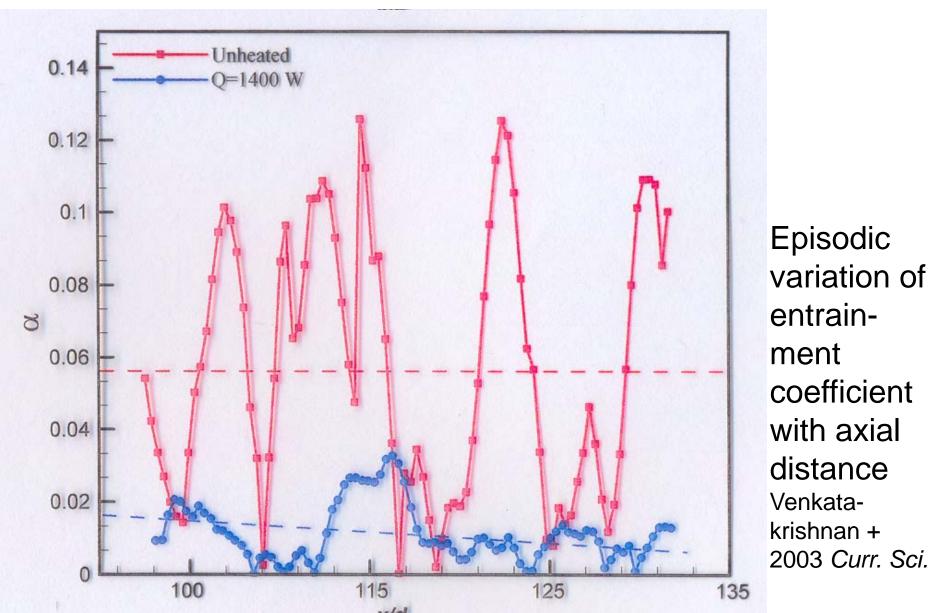


 Taylor's definition: Derived from self-similar flows (Morton et al 1956)

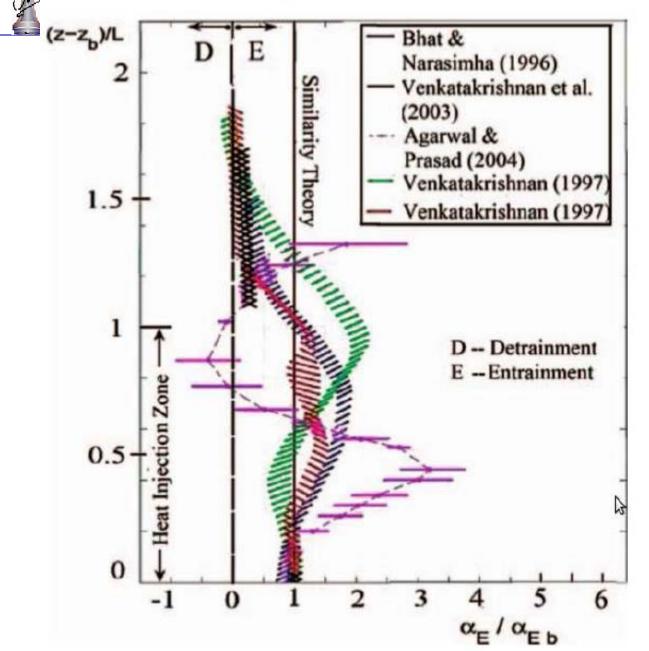
$$\frac{dm}{dz} = 2\pi b_u \alpha_e U_c$$



VARIATION OF ENTRAINMENT COEFFICIENT



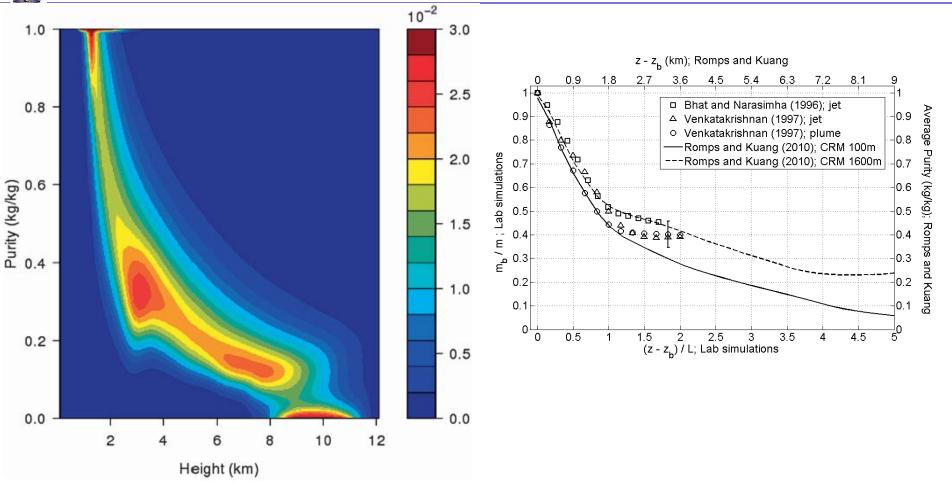
Previous Steady State Experiments



Diwan+ 2012



DILUTION AND PURITY



Romps & Kuang 2010 JAS

Comparison with Lab results (RN+2011PNAS)



A Cumulus Cloud Flow is a Special Example of a TRANSIENT DIABATIC PLUME

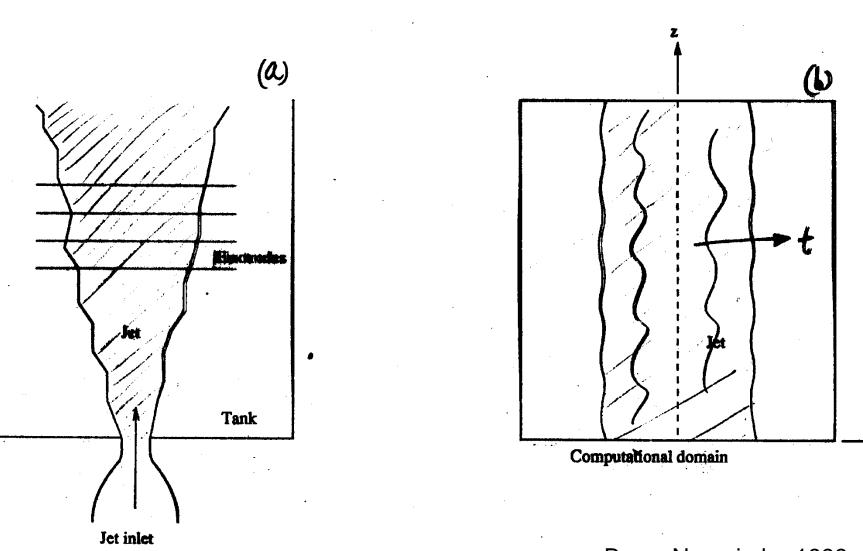


CYBER CLOUDS SPECTRAL METHODS

Code: Megha 1



LABORATORY VERSUS TEMPORAL SETUP SIMULATION



Basu, Narasimha 1999, JFM



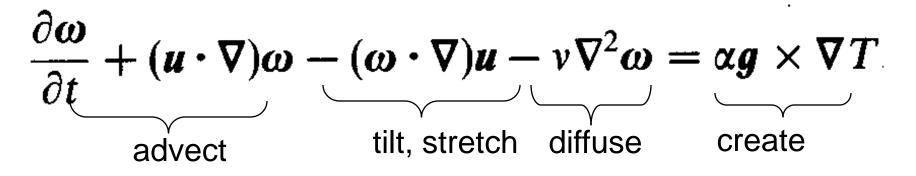
$$\nabla \cdot \boldsymbol{u} = \boldsymbol{0}, \qquad \text{(mass)}$$

$$\frac{\partial \boldsymbol{u}}{\partial t} + (\boldsymbol{u} \cdot \nabla)\boldsymbol{u} = -\frac{1}{\rho}\nabla p + \nu \nabla^2 \boldsymbol{u} - \boldsymbol{g}\alpha T, \qquad \text{(momentum)}$$

$$\frac{\partial T}{\partial t} + (\boldsymbol{u} \cdot \nabla)T = \kappa \nabla^2 T + \frac{J}{\rho c_p} H \qquad \text{(energy)}$$

Basu, RN 1999 J. Fluid Mech.



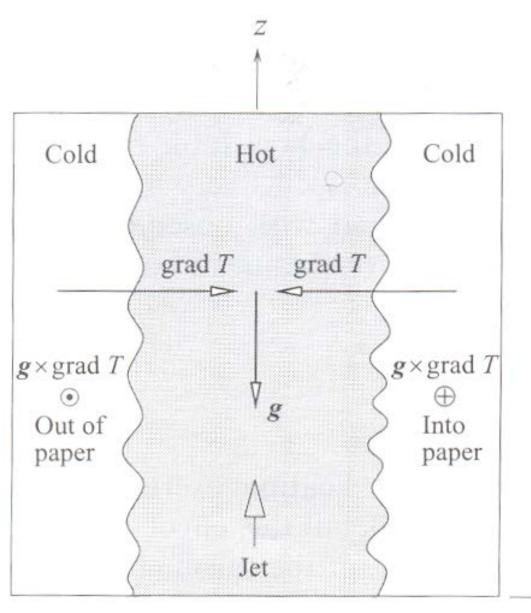


$$u(x,t) = u(x + Le_i, t), \quad p(x,t) = p(x + Le_i, t), T(x,t) = T(x + Le_i, t), \quad i = 1, 2, 3.$$

Basu, RN 1999 J. Fluid Mech.



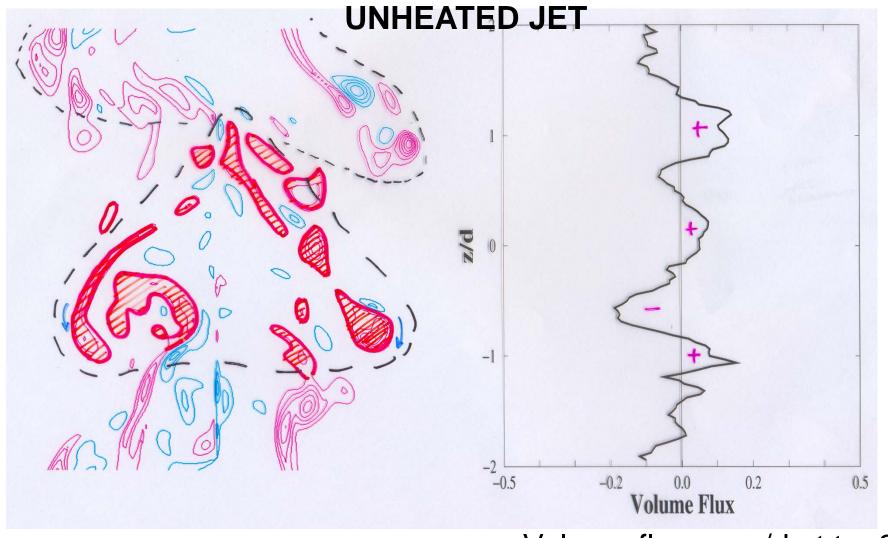
CREATING VORTICITY BY BAROCLINIC TORQUE



Basu, RN 1999 J. Fluid Mech.



COHRERENT STRUCTURE IN AZIMUTHAL VORTICITY



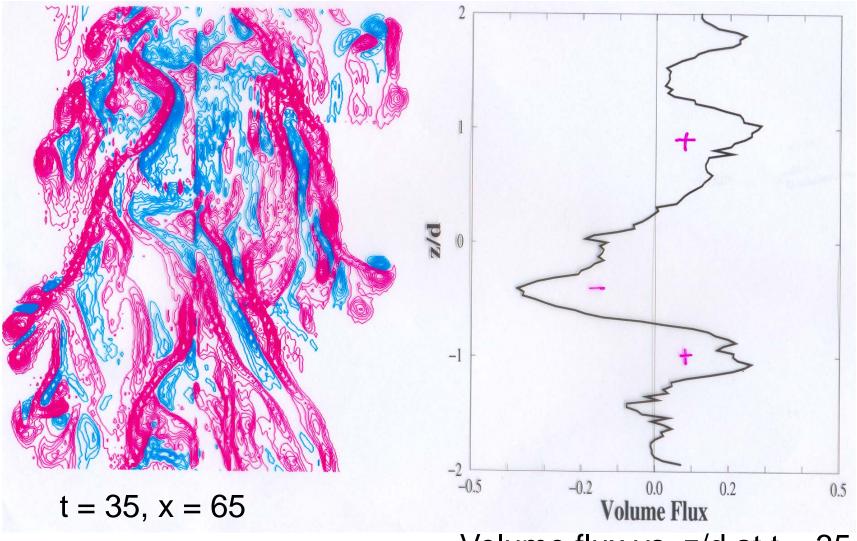
t = 35, x = 65

Volume flux vs. z/d at t = 35 RN, Shivakumar 1999 IUTAM Goettingen



AZIMUTHAL VORTICITY

FULLY HEATED JET

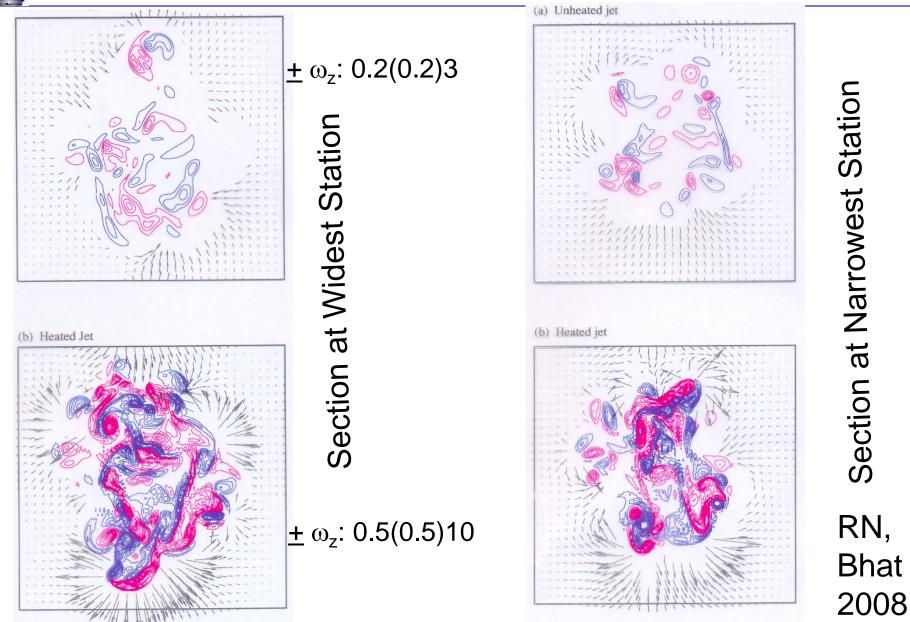


RN, Shivakumar 1999 IUTAM Goettingen

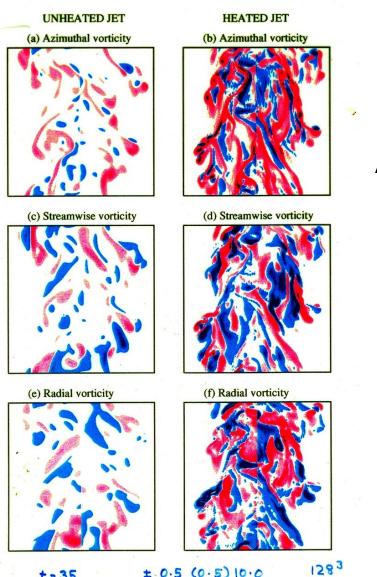
Volume flux vs. z/d at t = 35



UNHEATED, HEATED JETS



VORTICITY DISTRIBUTIONS



± 0.5 (0.5)10.0

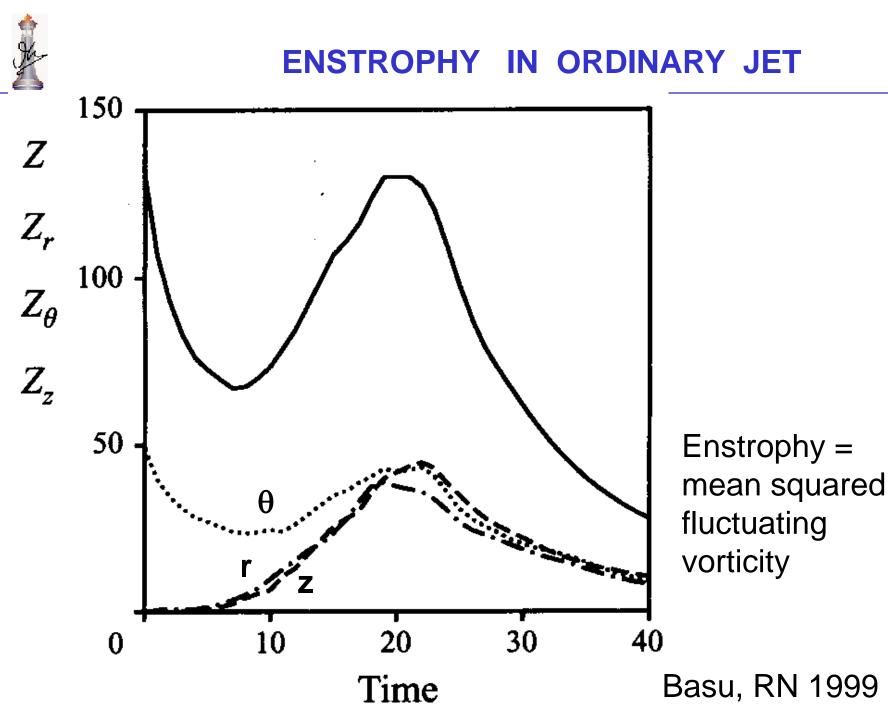
Left: Ordinary (Unheated), Right: Cloud (Heated)

Azimuthal

Axial

Radial

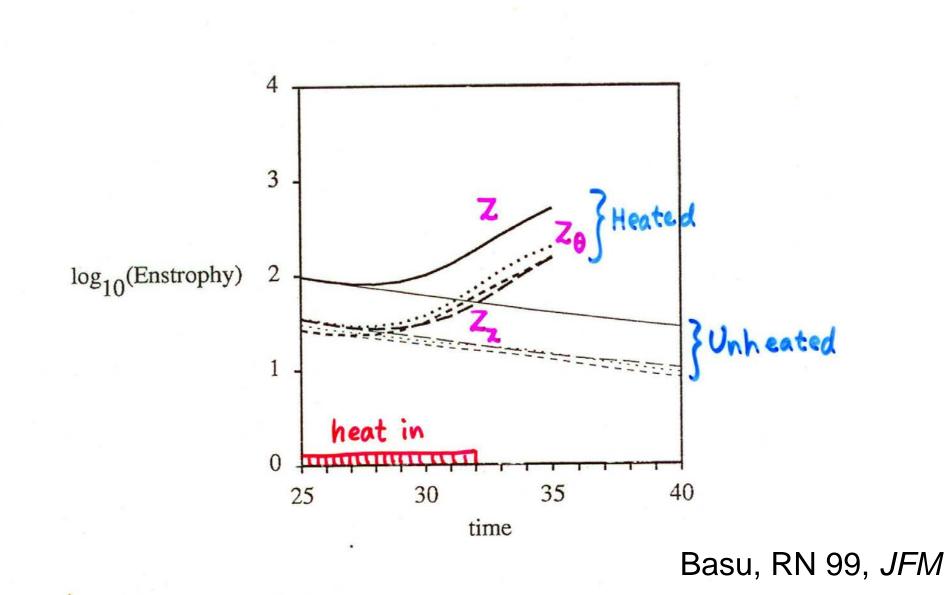
t=35



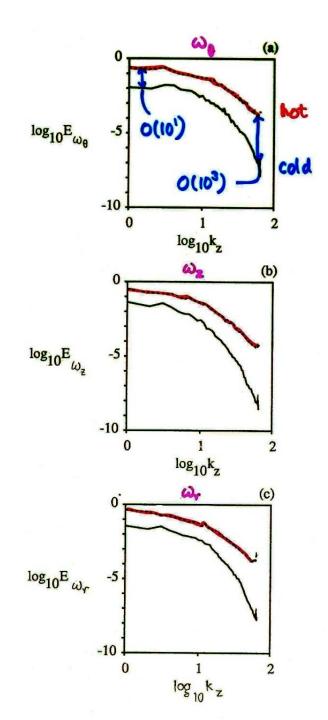
Basu, RN 1999 JFM



ENSTROPHY INCREASE WITH HEATING

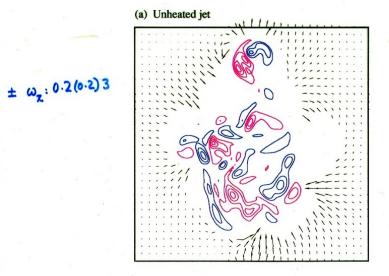






ENSTROPHY SPECTRA

SECTION AT WIDEST STATION



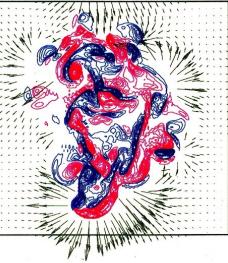
(a) Unheated jet

SECTION AT NARROWEST STATION

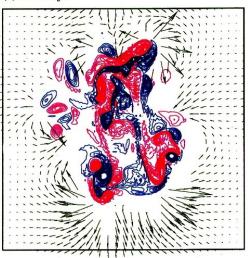
DIAMETRAL SECTIONS

(b) Heated Jet

± W2 : 0.5 (0.5) 10



(b) Heated jet





TRANSIENT DIABATIC PLUME

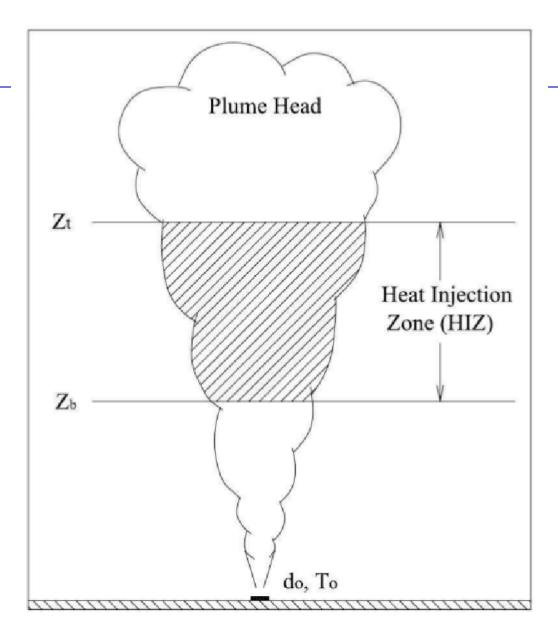
Megha 3

Prasanth++ 2014



Configuration

- d_o _ diameter of the source patch
- T_o source temperature above the ambient
- Z_b and Z_t vertical extent of the HIZ
- Horizontal extent of the HIZ is defined by a passive scalar (threshold value $\sim 10^{-4}$).





Direct Navier-Stokes-Boussinesq

- Reynolds number: 2000.
- Fractional-step method is used to solve the governing equations.
- Non-uniform grid, size 129×10^6 .
- Poisson solver: Preconditioned (multi-grid based) GMRes.



Exploratory runs

- Domain Size: 40 x 40 x 40 (x y z)
- Grid: 128 x 128 x 256 ~ 4 x 10⁶ cells

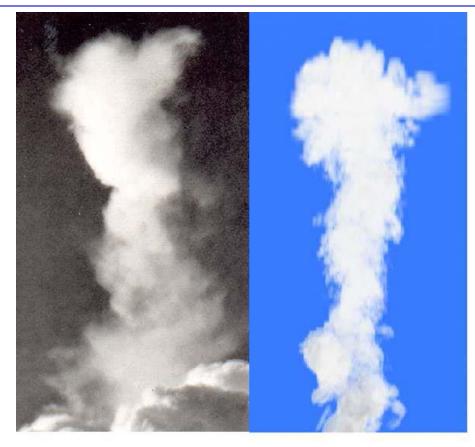
Resolved Simulation

- Domain Size: 70 x 70 x 39.9 (x y z)
- Grid: 402 x 402 x 798 ~ 129 x 10⁶ cells

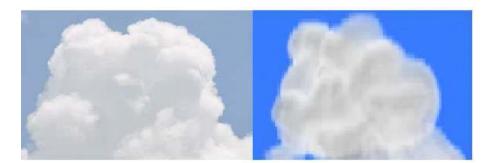
Common parameters

- Reynolds No : 2000
- 10% noise added to the temperature source (z = 0)

COMPARISON OF CLOUD SHAPES Real Cyber

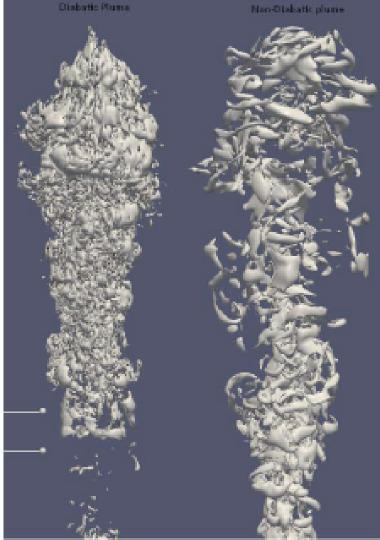


- Re = 2000
- Pr = 1.0
- $\Delta t = 0.005$
- Grid: 128 x 128 x 256
- HIZ: Z_b = 10d, Z_t = 15d
- Volumetric visualisation using PARAVIEW.





Vorticity Iso surface



VORTICITY EXPLODES WITH HEATING

Left: With heating, iso-surface at 2.5

Right: No heating , iso-surface at 0.75

Baroclinic torque spins up cloud

t = 59.5 flow units Azimuthal Component (-2.5)

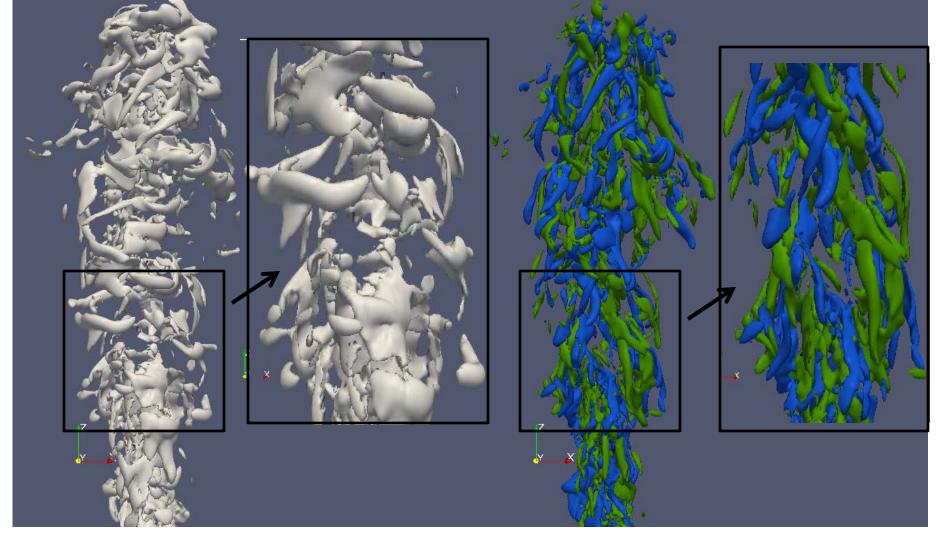
t = 127.5 flow units Azimuthal component (-0.75)



Vorticity iso surface for plumes

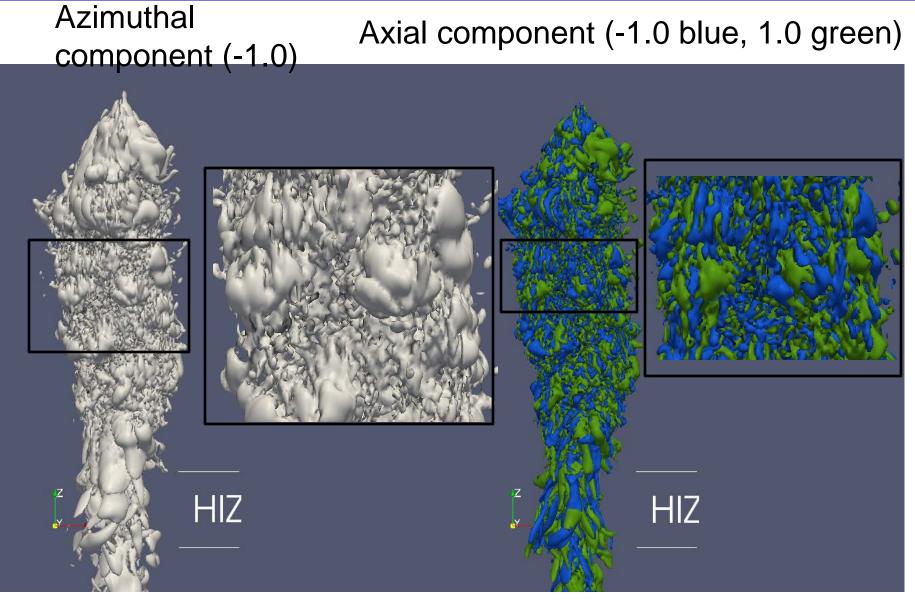
Azimuthal component (-1.0)

Axial component (-1.0 blue, +1.0 green)

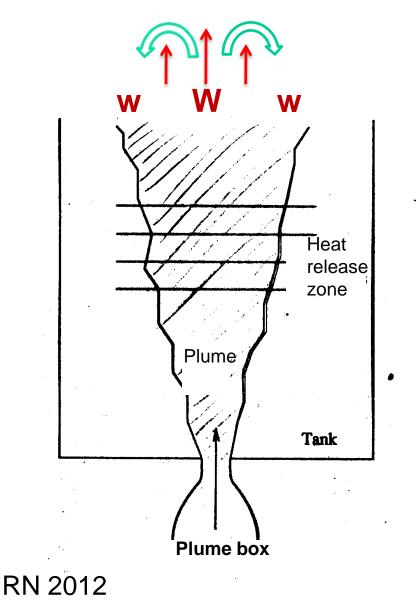




Vorticity iso surface for cloud flow







The Baroclinic Torque The varying buoyancy force Temperature gradient

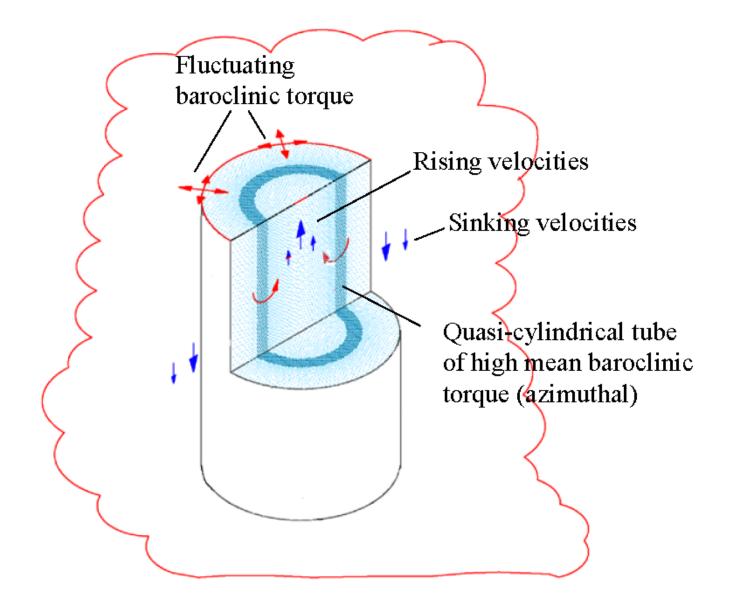
The baroclinic torque is proportional to the temperature gradient, so is a maximum mid-way between cloud centre and edge

There is a quasi-cylindrical tube of maximum baroclinic torque embedded within the cloud flow

The fluctuating baroclinic torque is a huge source of small-scale vorticity. Could that be what makes some cumulus clouds so crinkly at the edges ?



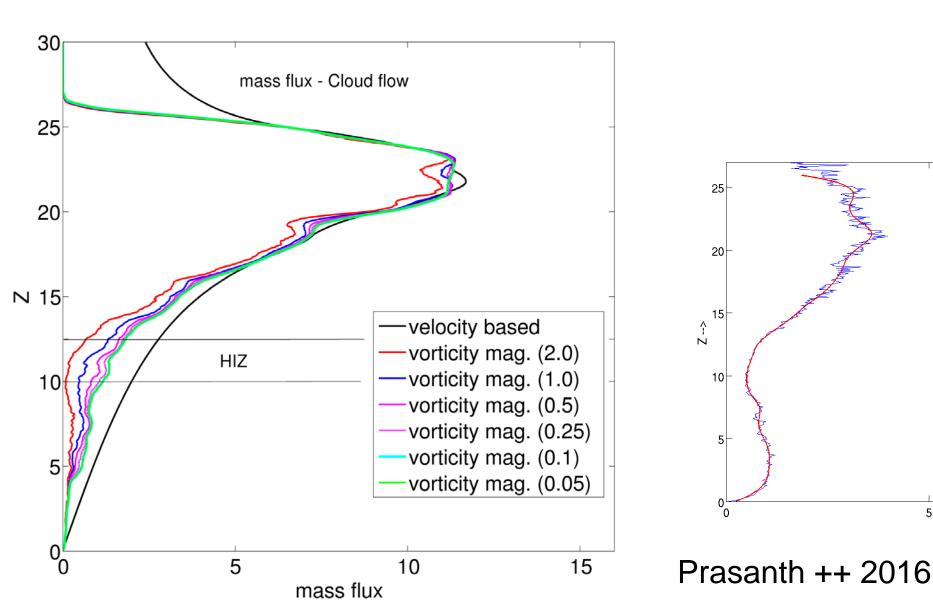
HOW THE BAROCLINIC TORQUE WORKS





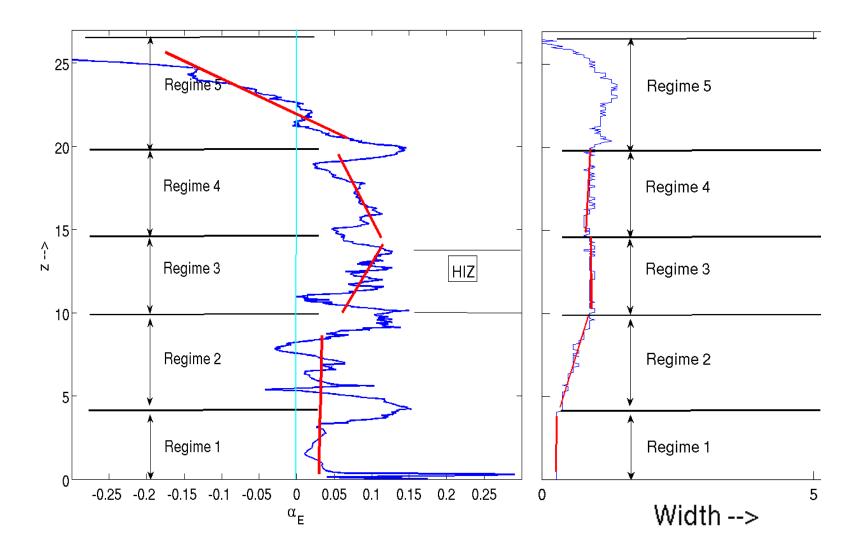
WHAT IN-CLOUD MASS FLUX?

5





Entrainment coefficient and width





Re = 2000 Totally 90 FU HIZ : 10 – 15 diameters Heating stops at 65 FU

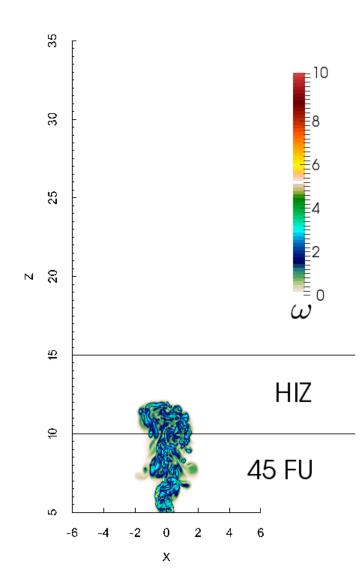
Samrat Rao++ 2016



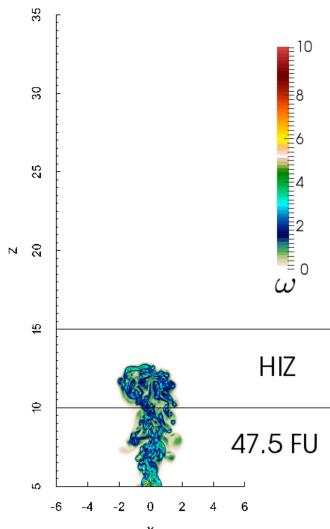


Axial sections at y = 0



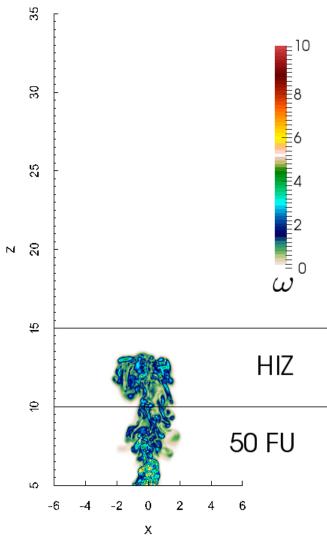




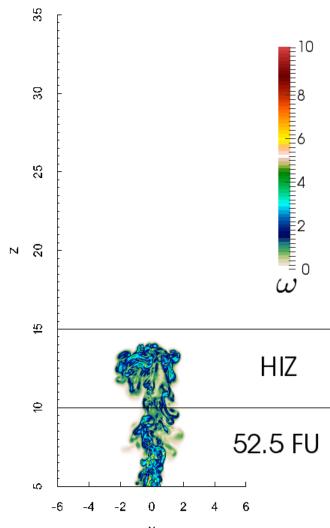


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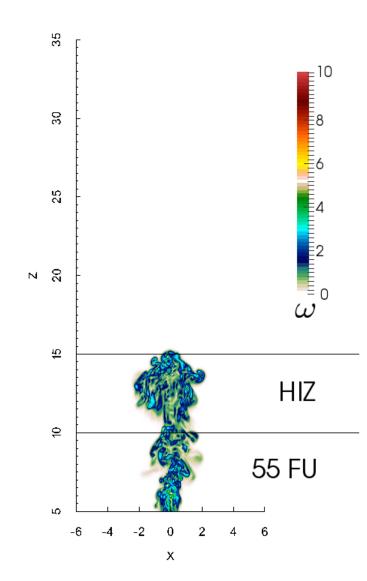




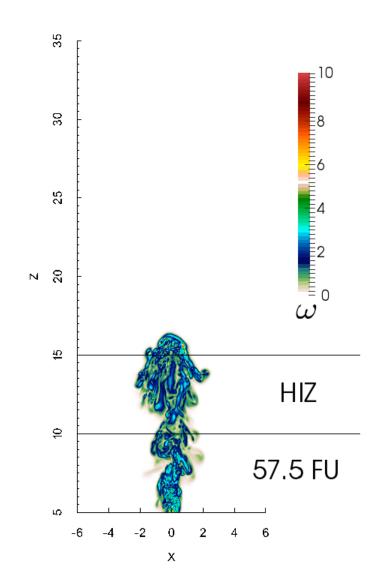


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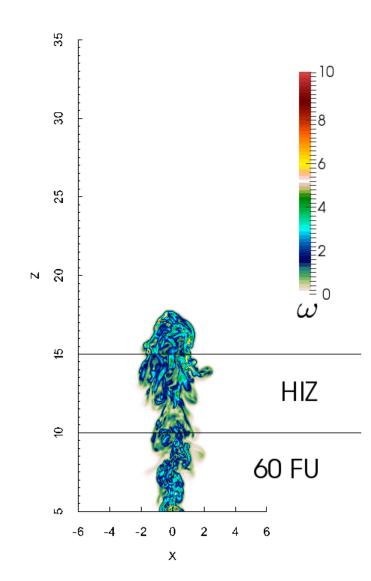




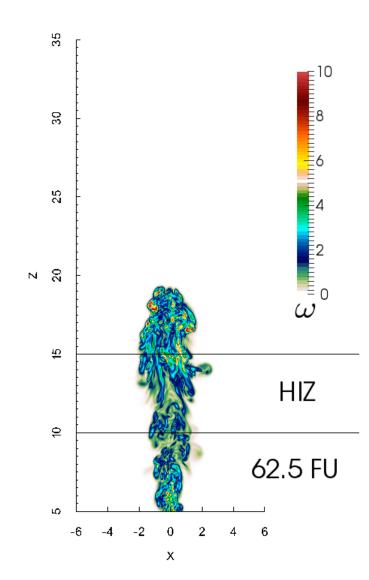




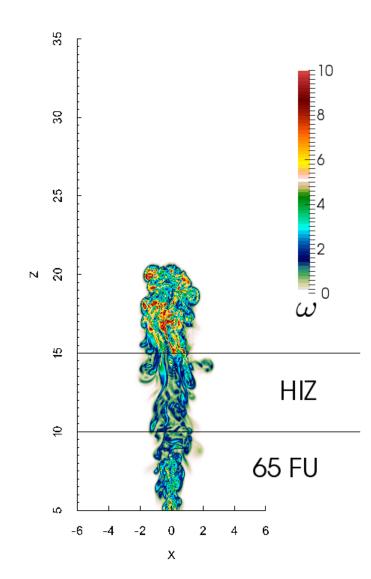




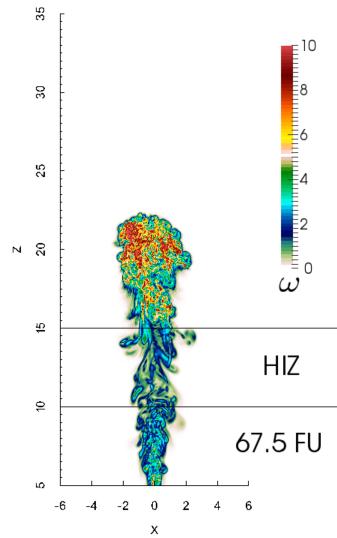




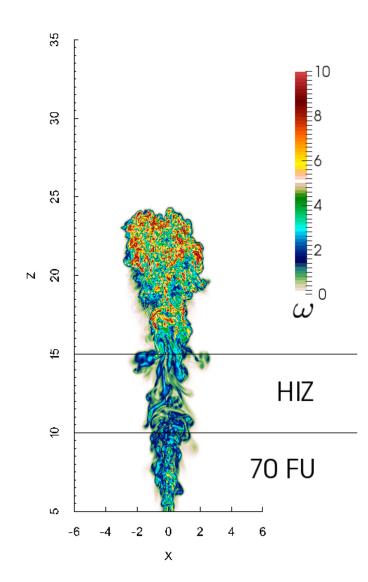




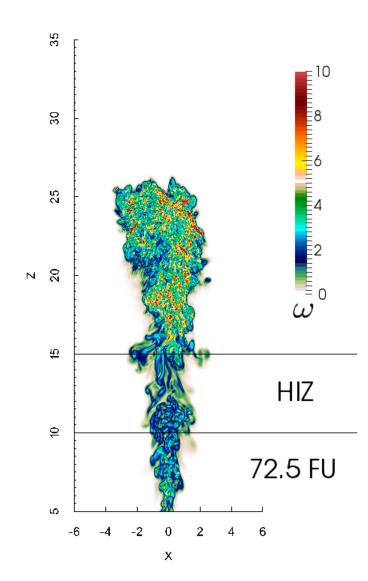




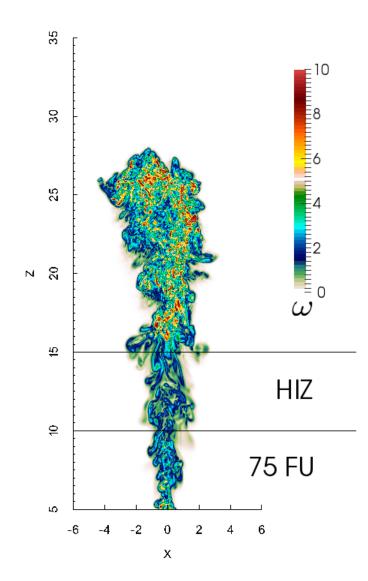




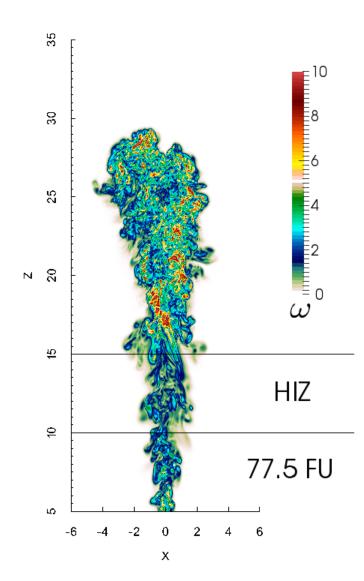




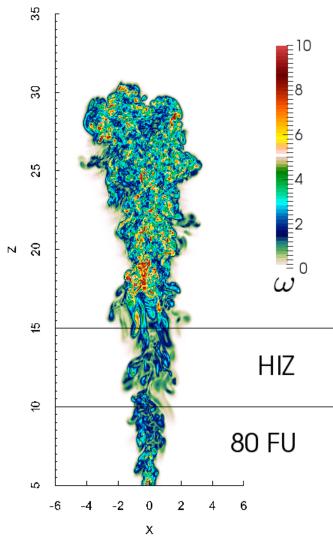




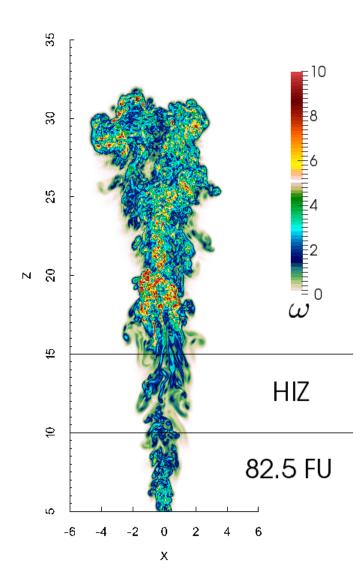




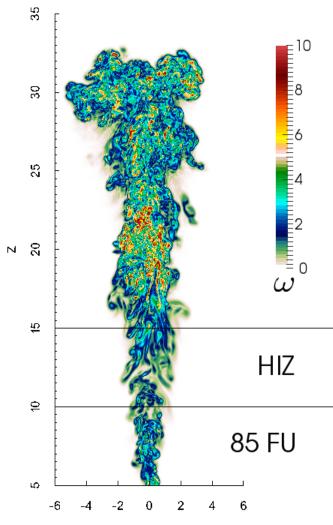




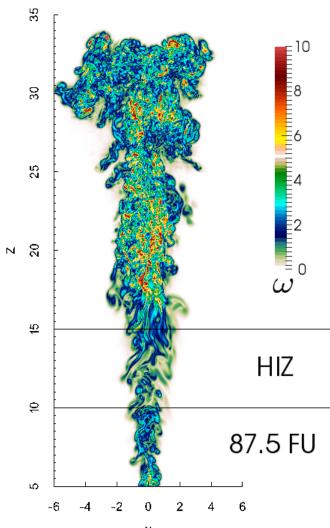






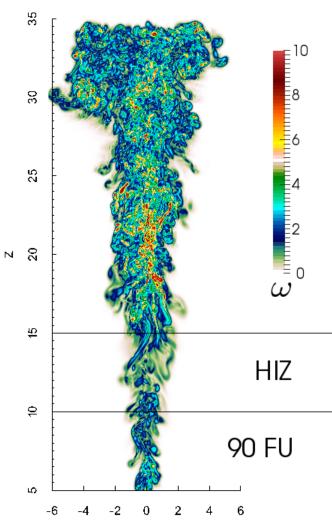






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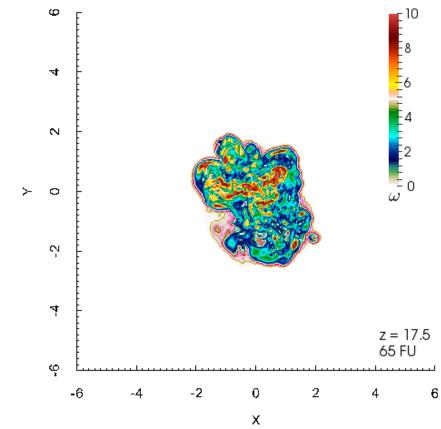
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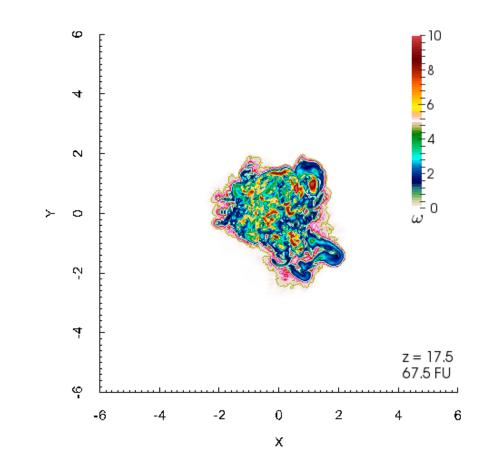
Diametral cross-sections

at z = 17.5, with time

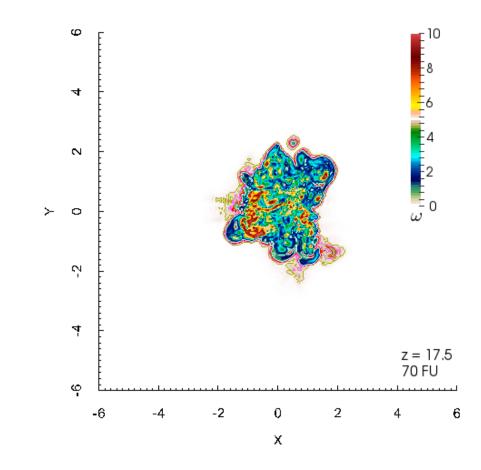




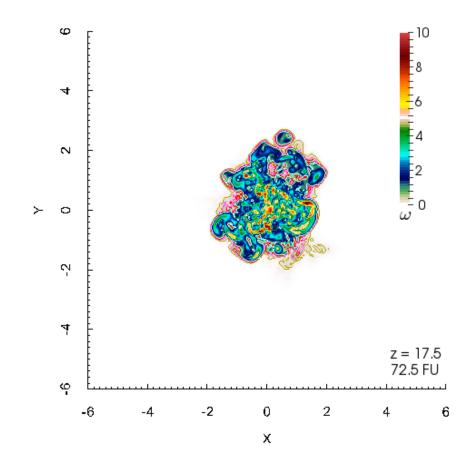




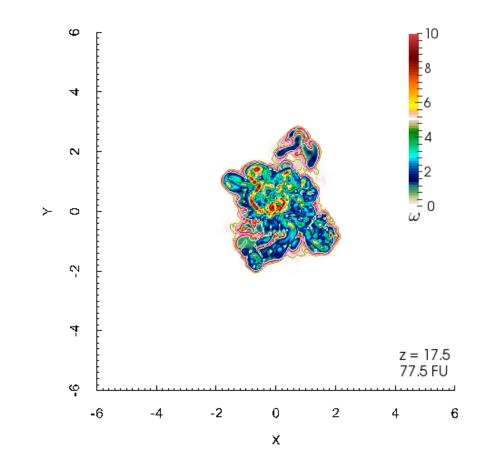




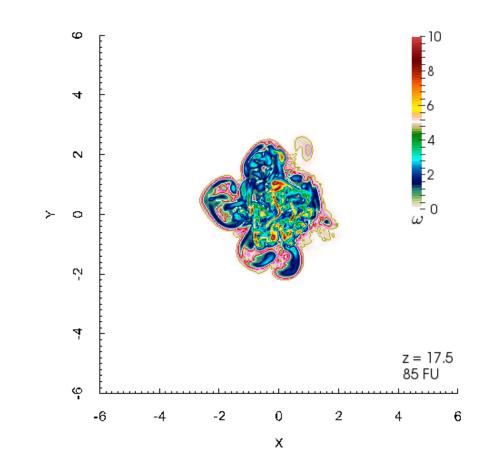










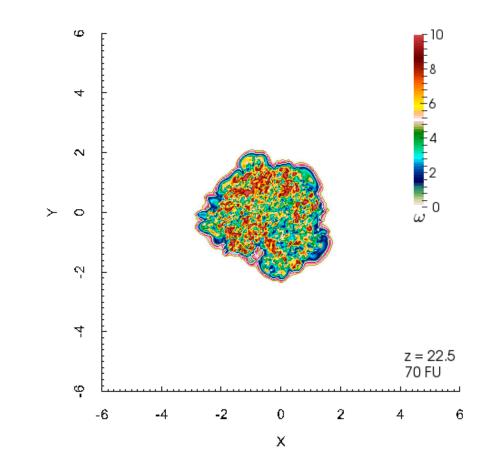




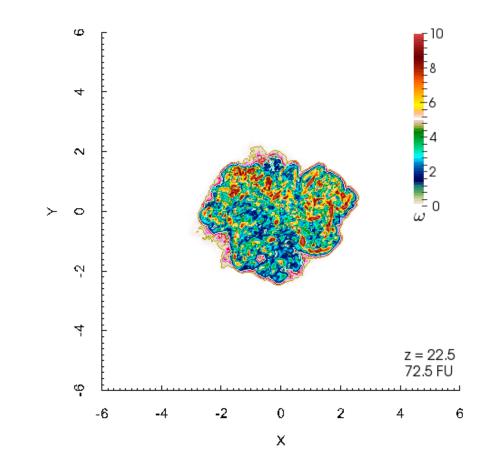
Diametral cross-sections

at z = 22.5, with time

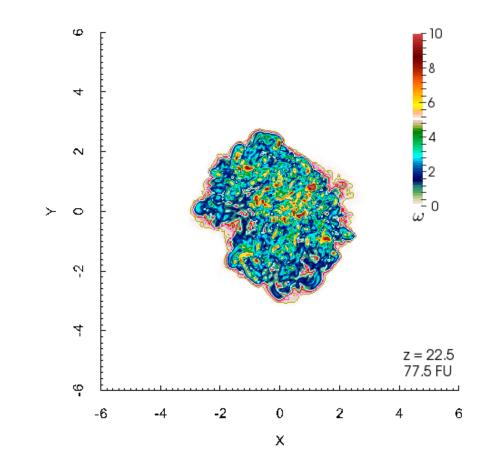




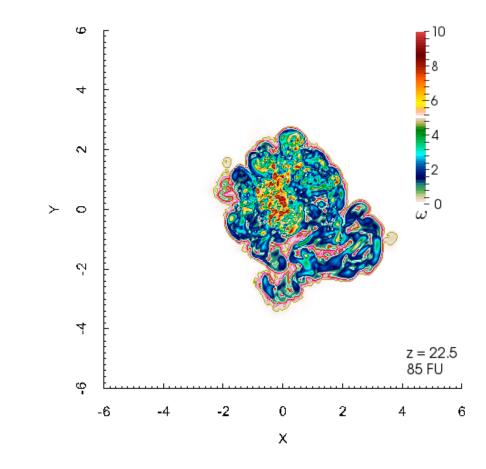










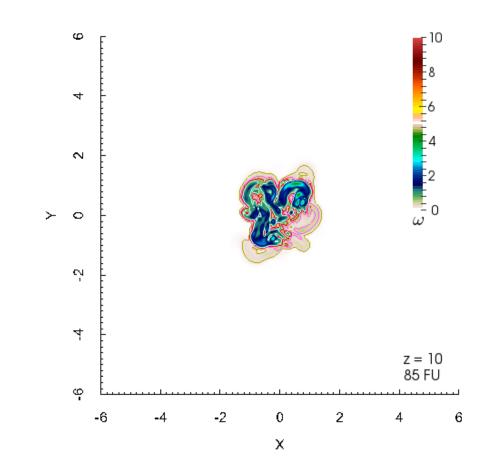




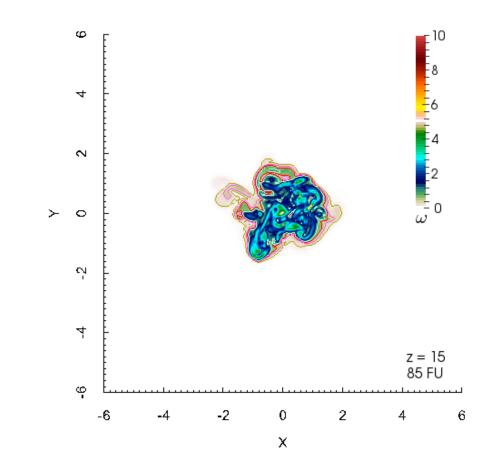
Diametral cross-sections

at 85 FU, with z

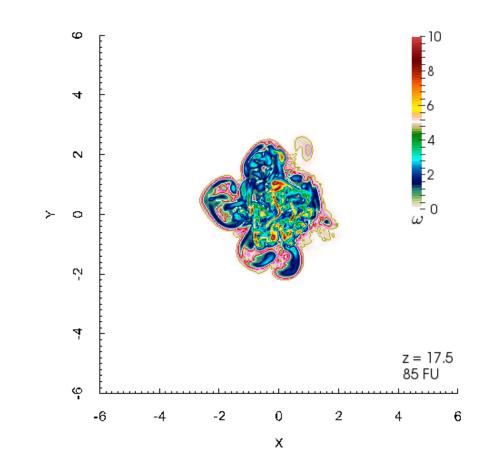




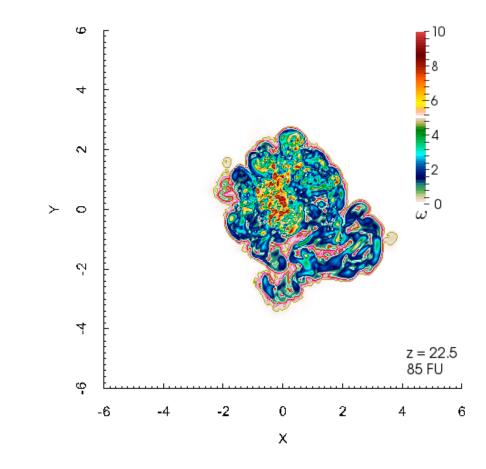




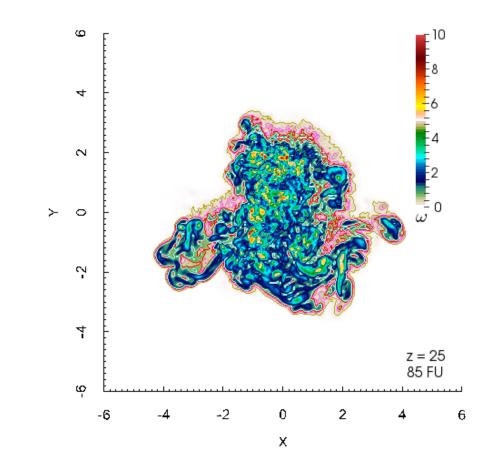




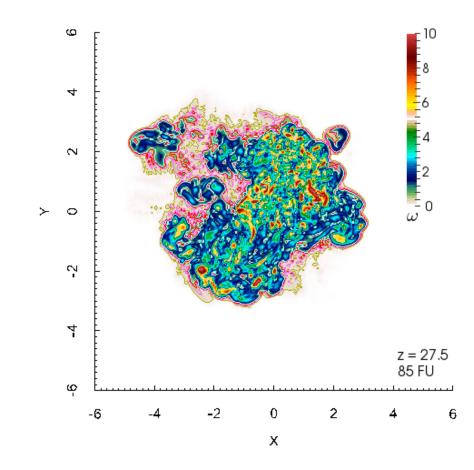




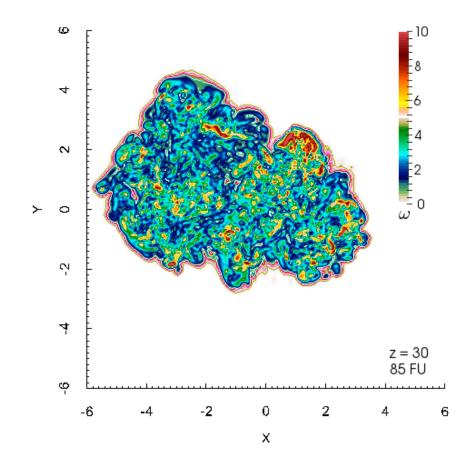








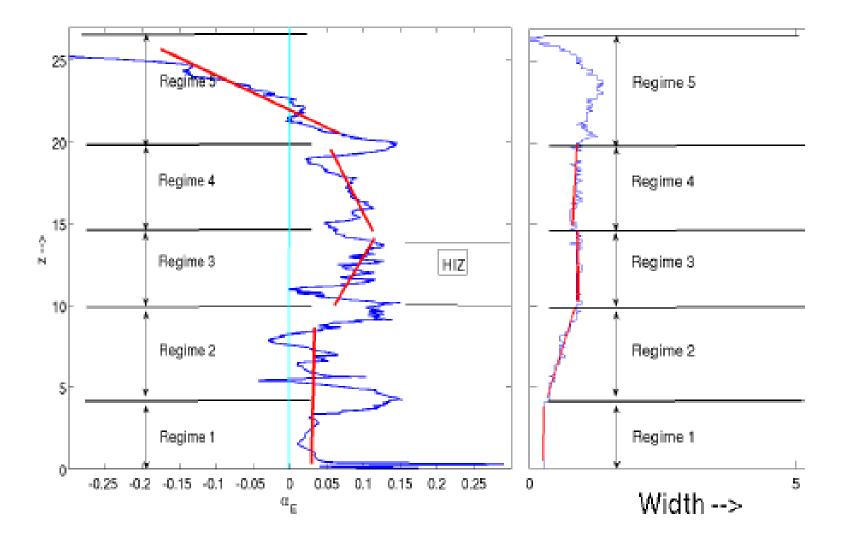








Entrainment coefficient and width





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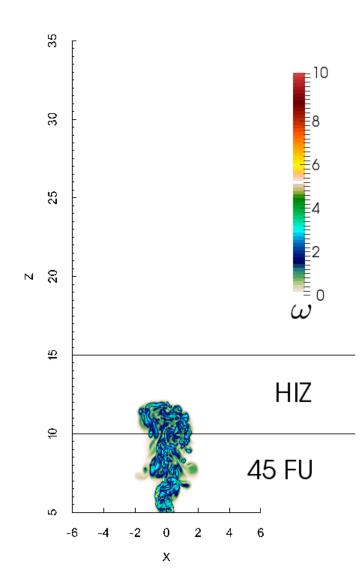


HEATING PROFILE HISTORY

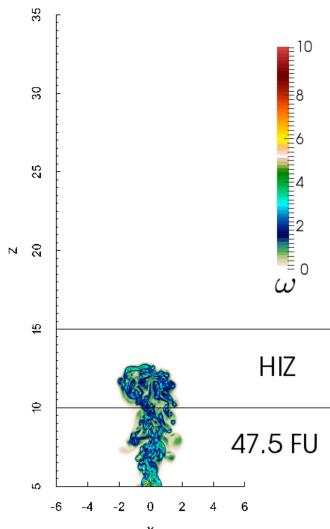


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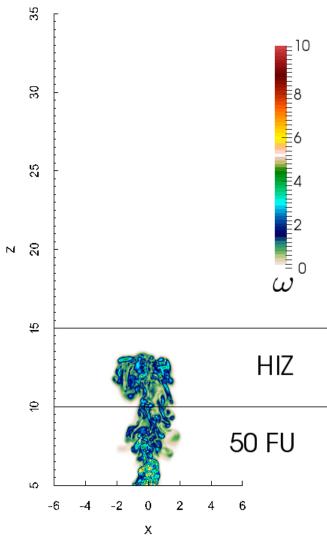




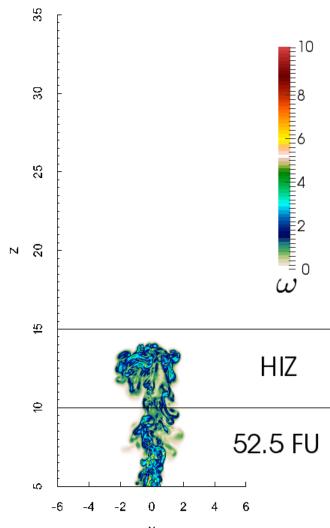


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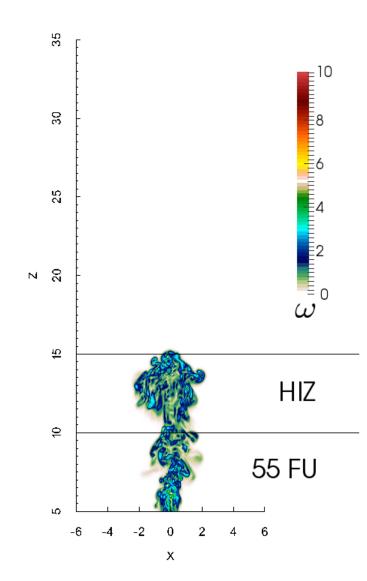




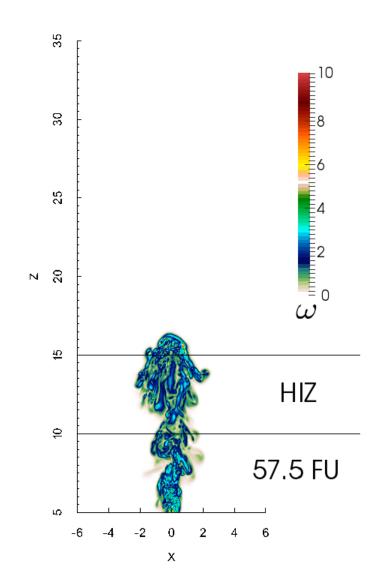


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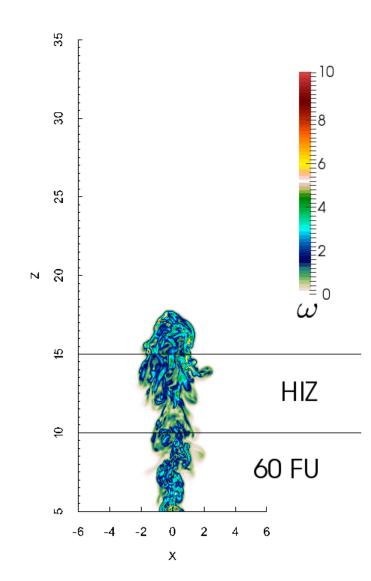




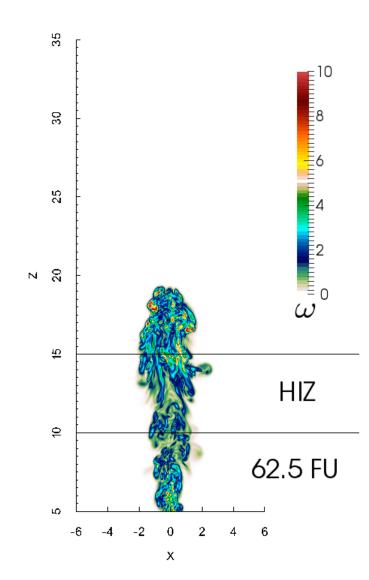




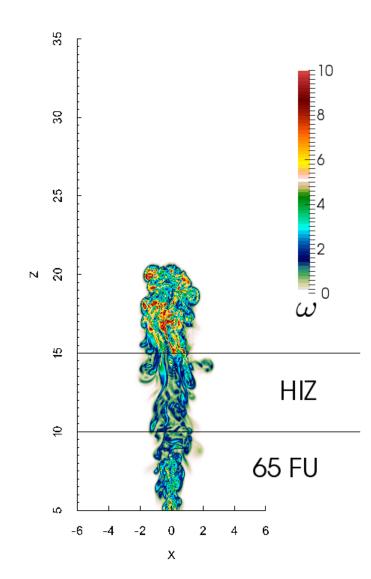




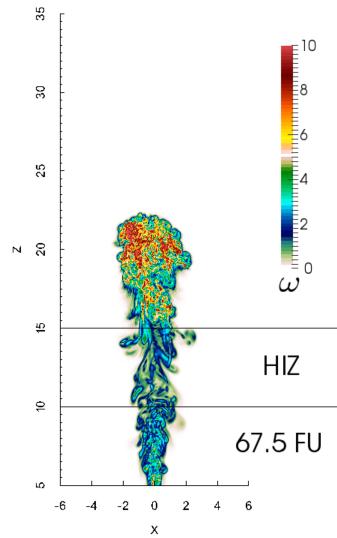




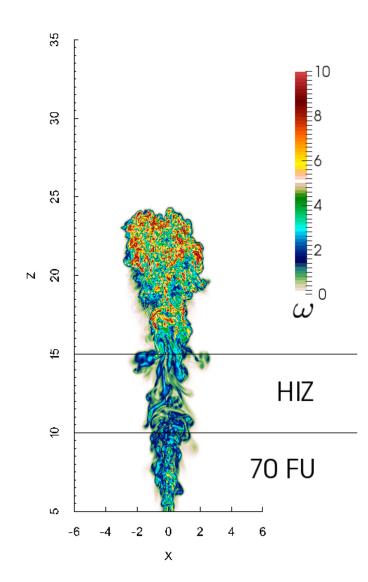




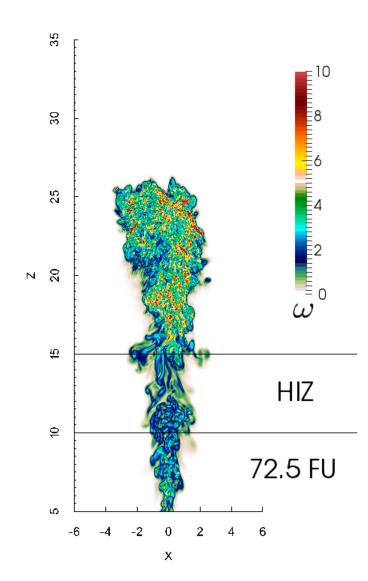




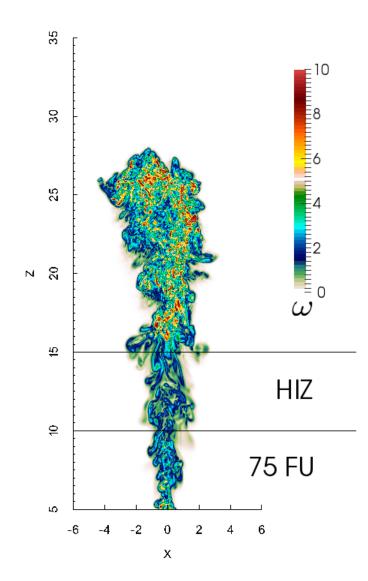




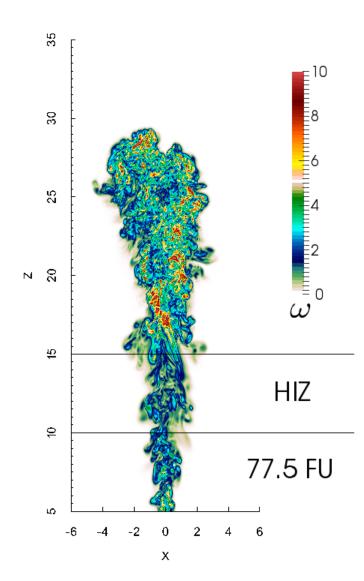




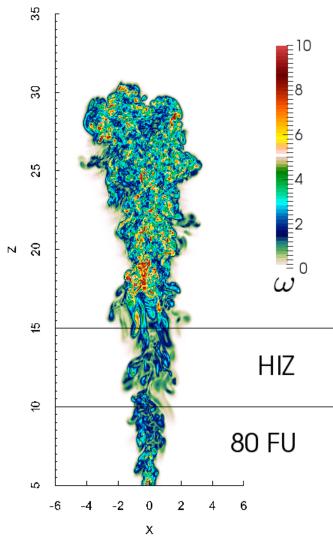




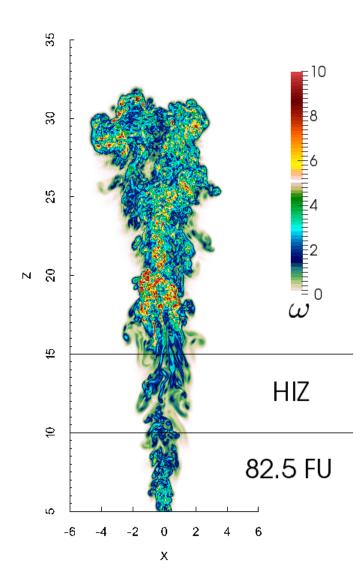




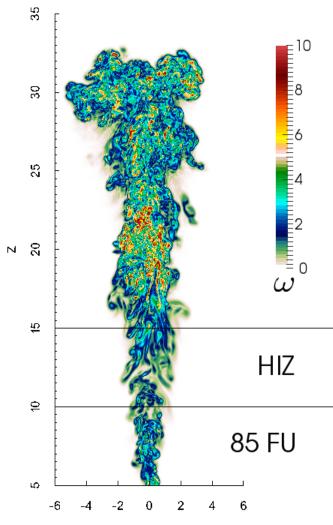




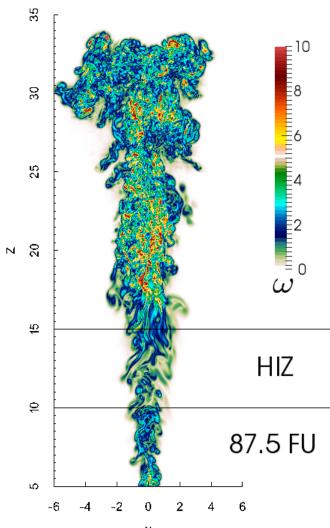






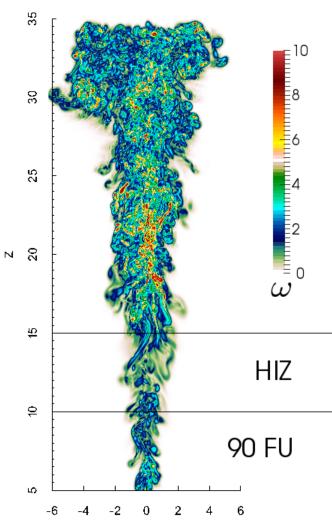






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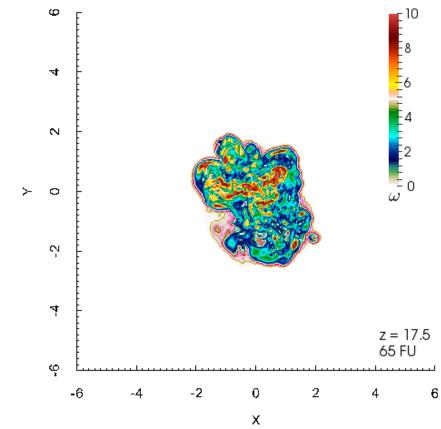
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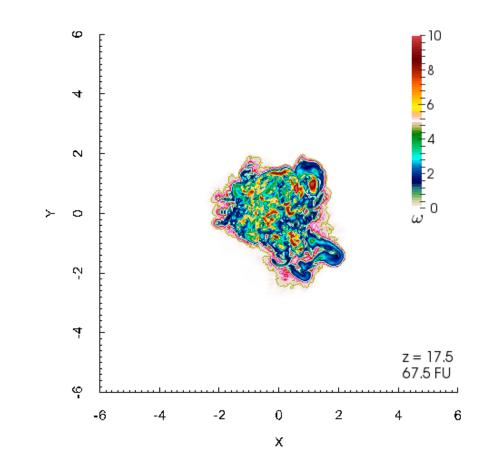
Diametral cross-sections

at z = 17.5, with time

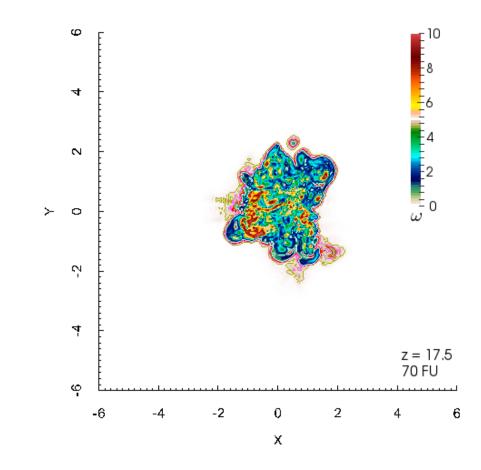




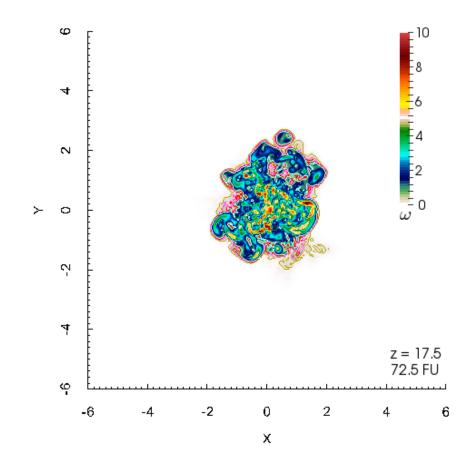




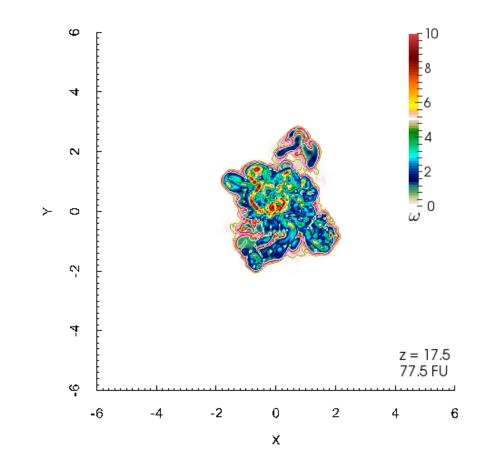




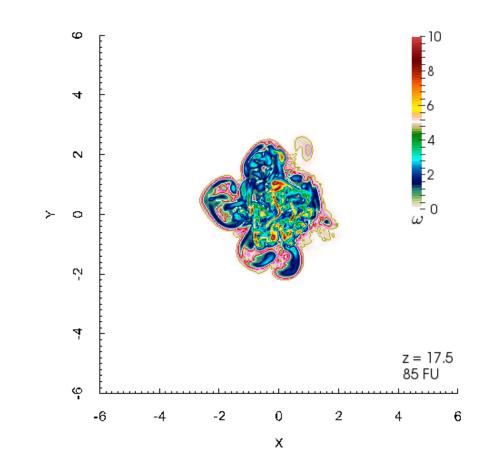










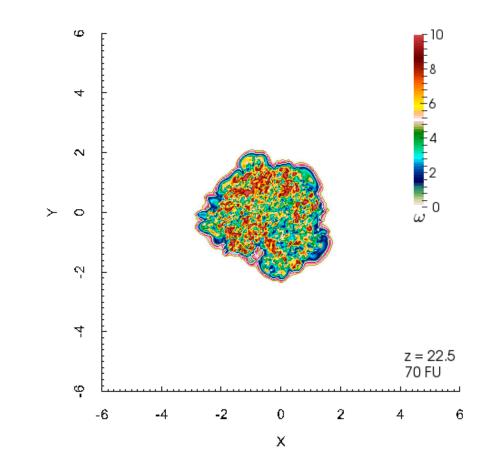




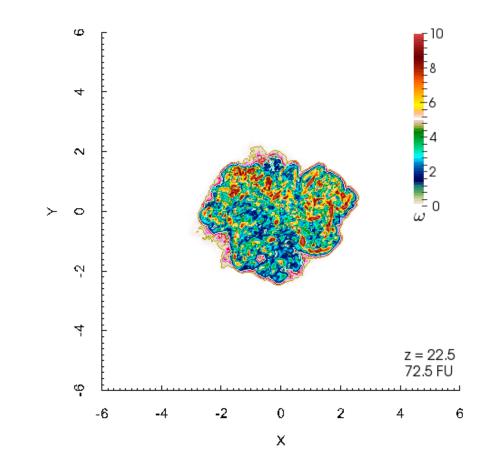
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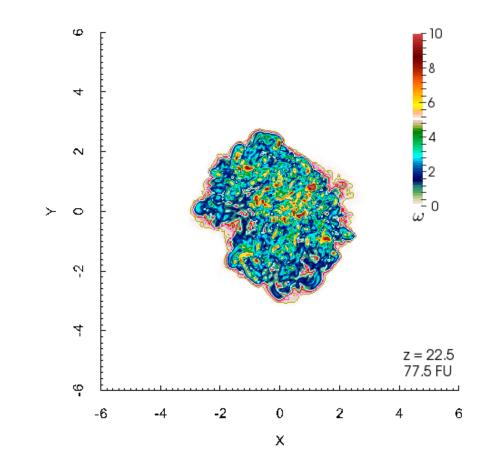




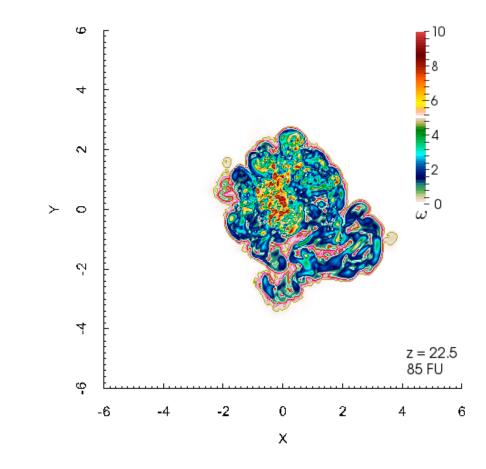










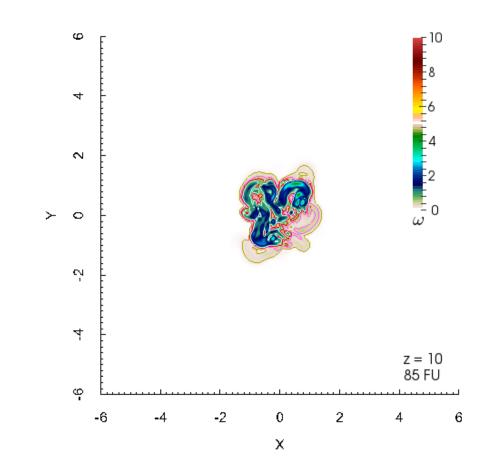




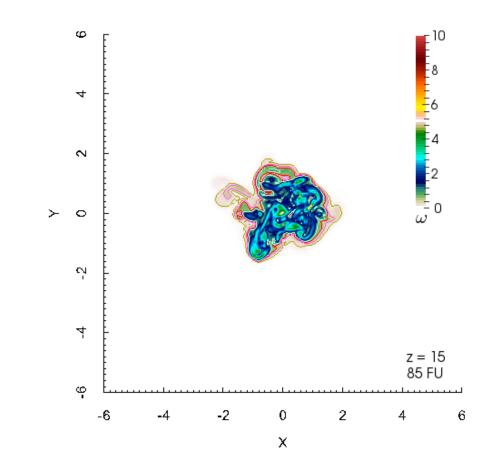
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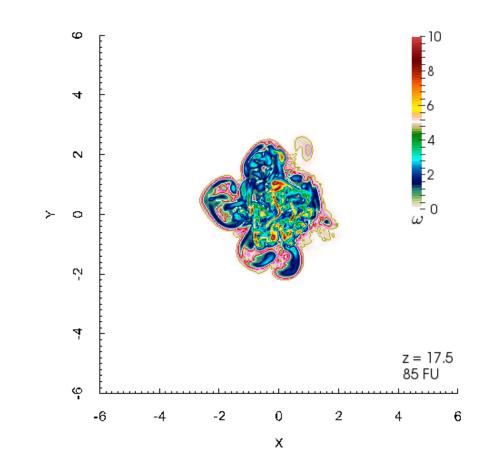




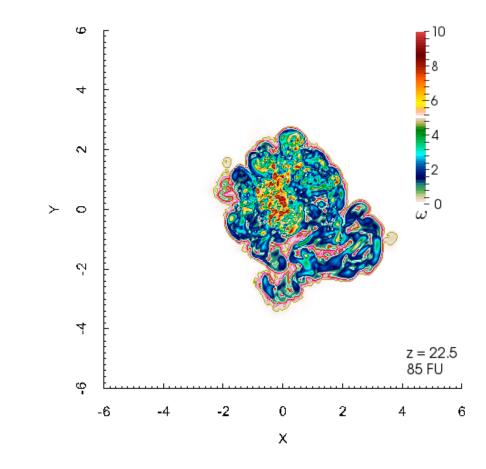




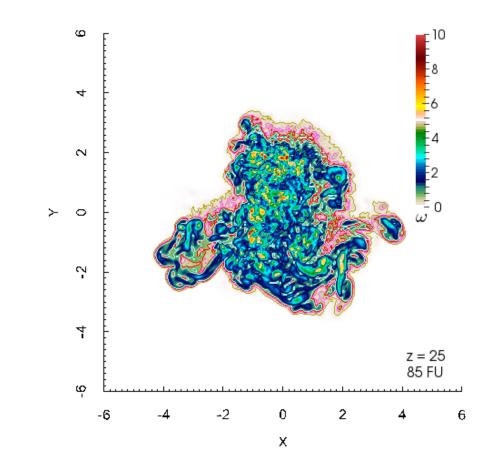




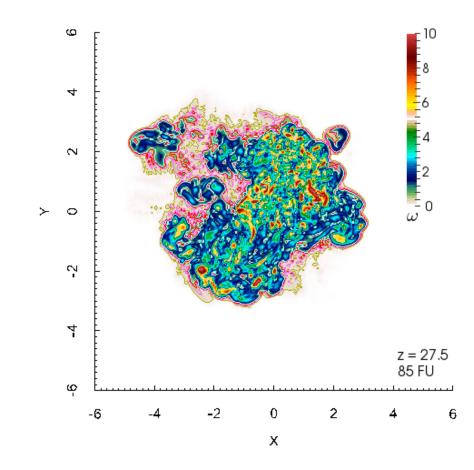




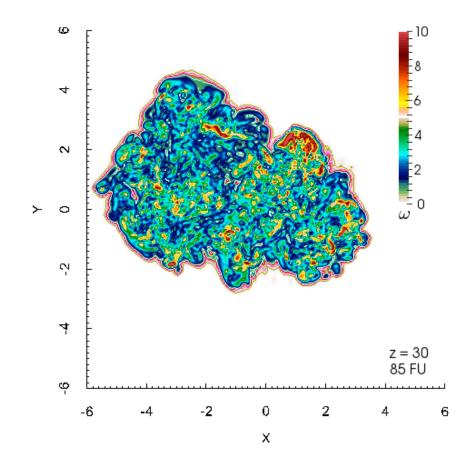












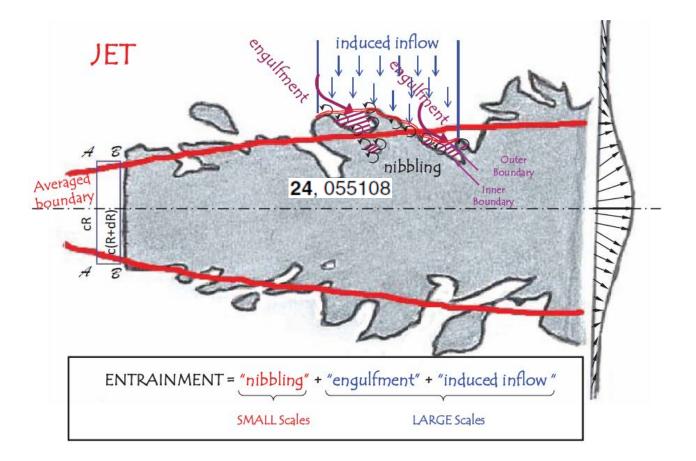


THE ENTRAINMENT PROCESS





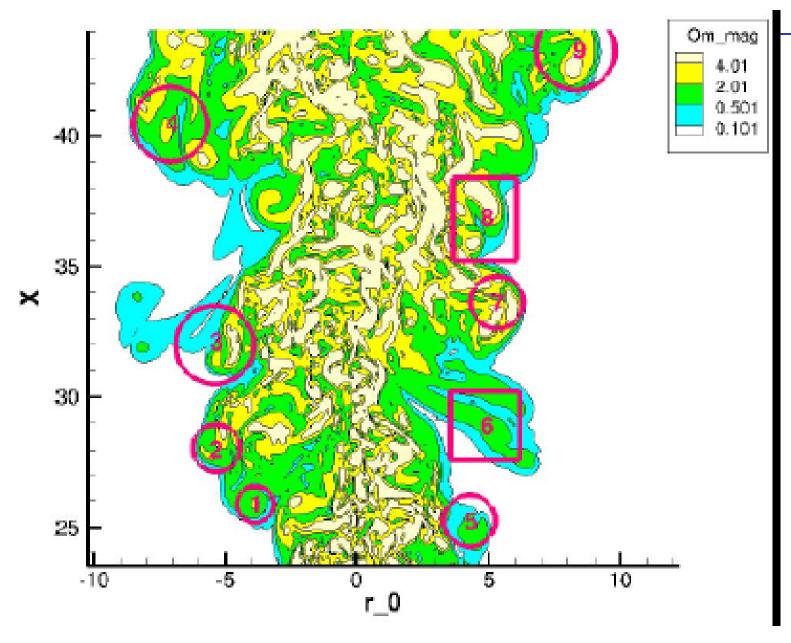
ONE VIEW OF ENTRAINMENT



Philip and Marusic, 2012, PoF 24

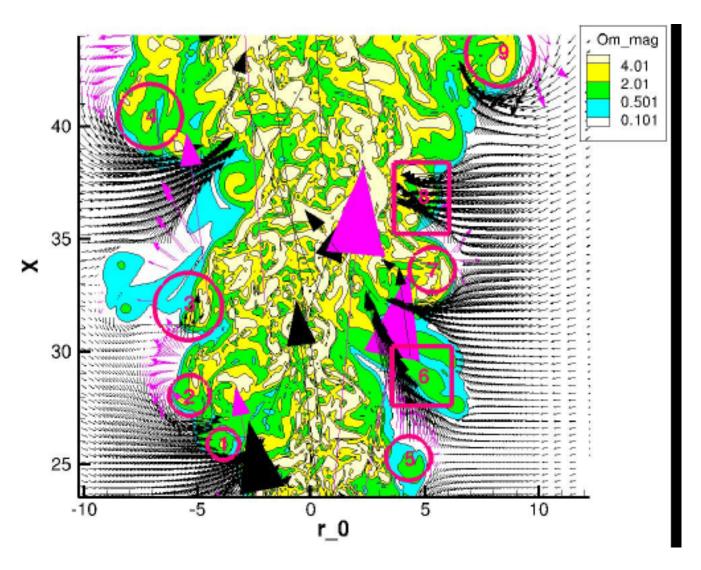


AXIAL Section : Vorticity field



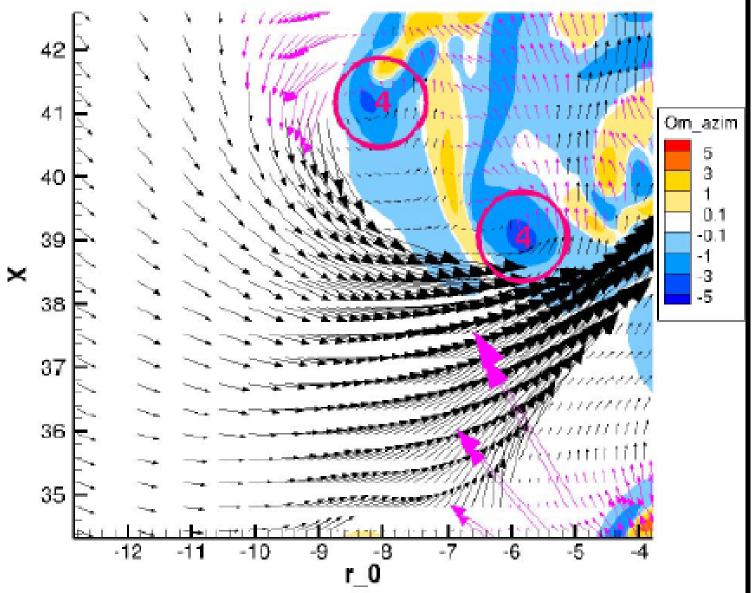


ANOTHER VIEW OF ENTRAINMENT



AXIAL Section : Velocity & Vorticity fields







PROPOSED VIEW OF THE ENTRAINMENT PROCESS

- Largely episodic in both time and space . . .
- with local inrush events, induced in the ambient outer fluid by neighbouring vorticity elements of coherent structures within the core flow, –...
- In the second second
- ... creating a strong 'engulfing event'...
- . . .that culminates in fluid crossing the T/NT interface in the well – through 'nibbling' (?).
- Entrainment coefficients vary greatly from Turner's similarity value and . . .
- ✤ . . . are strongly affected by heat release, . . .
- ✤ . . . which creates a baroclinic torque . . .



PROPOSED VIEW OF THE ENTRAINMENT PROCESS

- ✤ . . . that leads to an explosive growth in vorticity, . . .
- . . .disrupts the coherent structures that would have filled the non-diabatic flow . . .
- ... and changes the nature of inrush events ...
- ✤ . . . which affects entrainment. . . .
- ✤ . . . And so on!



Conclusions



- Cumulus clouds are generally transient flows
- Latent heat release on condensation of water vapour changes an ordinary plume into a cloud-like flow
- So a transient diabatic plume seems like a good fluiddynamical model for cumulus flow
- Measurements in transient diabatic plumes show systematic but wide variations in entrainment coefficient with cloud height. Reason for great variety of proposals made over decades that have all 'seemed' based on 'fact' ?
- Computer simulations suggest that the baroclinic torque drives the cumulus flow engine



Conclusions continued.....

- 3D Navier-Stokes-Boussinesq solver capable of simulating cloud flow developed and validated.
- Significant role played by heating profile history in determining the shape of any cumulus flow.
- Strong effect of off-source buoyancy addition and baroclinic torque on the structure of the flow
- 5 distinct regimes:
 - 1. A nearly laminar constant width regime
 - 2. A nearly linearly growing turbulent plume regime
 - 3. HIZ where the width is nearly constant
 - 4. A regime of slow growth in width culminating at the maximum
 - 5. A short dome like cloud top
- Preliminary estimates on the entrainment coefficient.



Real Cloud Cyber Cloud Laboratory Cloud

NOAA Research, Jim Lee

RN ++ 2011 PNAS

Present Simulation



Acknowledgements

CO-WORKERS

- Prof K R Sreenivas
- Prof S M Deshpande
- Prof G S Bhat
- Prof A Prabhu
- Dr R Elavarasan
- Dr L Venkatakrishnan
- Dr S Duvvuri
- Dr S Diwan
- Dr A Konduri
- Mr P Prasanth
- Dr Sachin Shinde

- Dr Samrat Rao
- Mr G Vybhav Rao
- Mr S Ravichandran

SUPPORT

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- Prof P Seshu, Dr. U N Sinha at CMMACS / 4PI
- Dr Rajat Moona, CDAC
- Profs N Balakrishnan,
 - R Govindarajan, SERC, IISc



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- Diwan et al. 2014 BAMS



THANK YOU FOR LISTENING !